



Vibration Energy Harvesting using Multi-Frequency and Nonlinear Piezoelectric Converters

Vittorio Ferrari



Department of Information Engineering
University of Brescia - ITALY



- Acknowledgments and credits to:
 - ◆ Davide Alghisi
 - ◆ Marco Ferrari
 - ◆ Marco Baù
 - ◆ Michele Guizzetti
 - ◆ Simone Dalola
 - ◆ Daniele Marioli
 - ◆ Marco Demori
 - ◆ Emanuele Tonoli

Contents

- Introduction
- Multi-frequency piezoelectric harvester arrays
- Nonlinear piezoelectric harvesters
- Conclusions

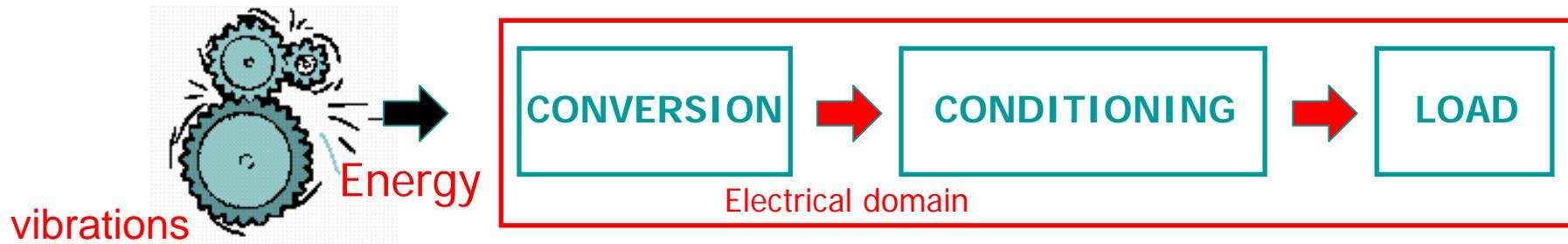


Contents

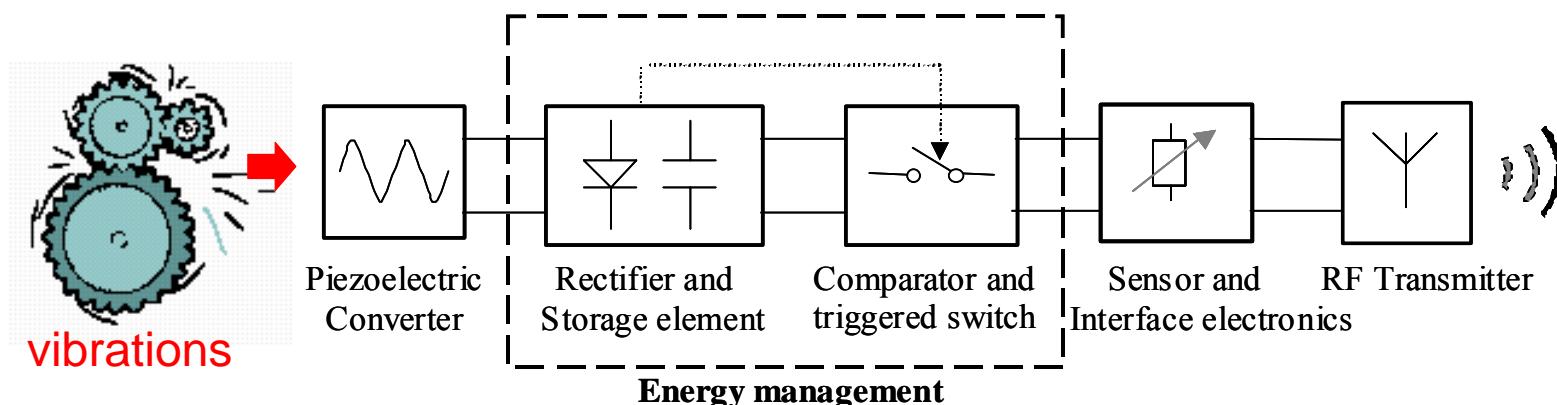
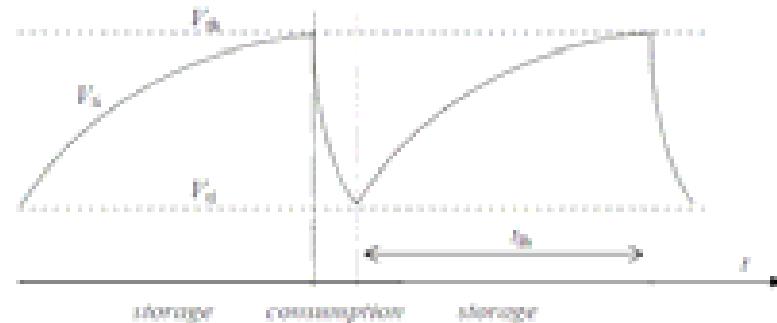
- Introduction
- Multi-frequency piezoelectric harvester arrays
- Nonlinear piezoelectric harvesters
- Conclusions



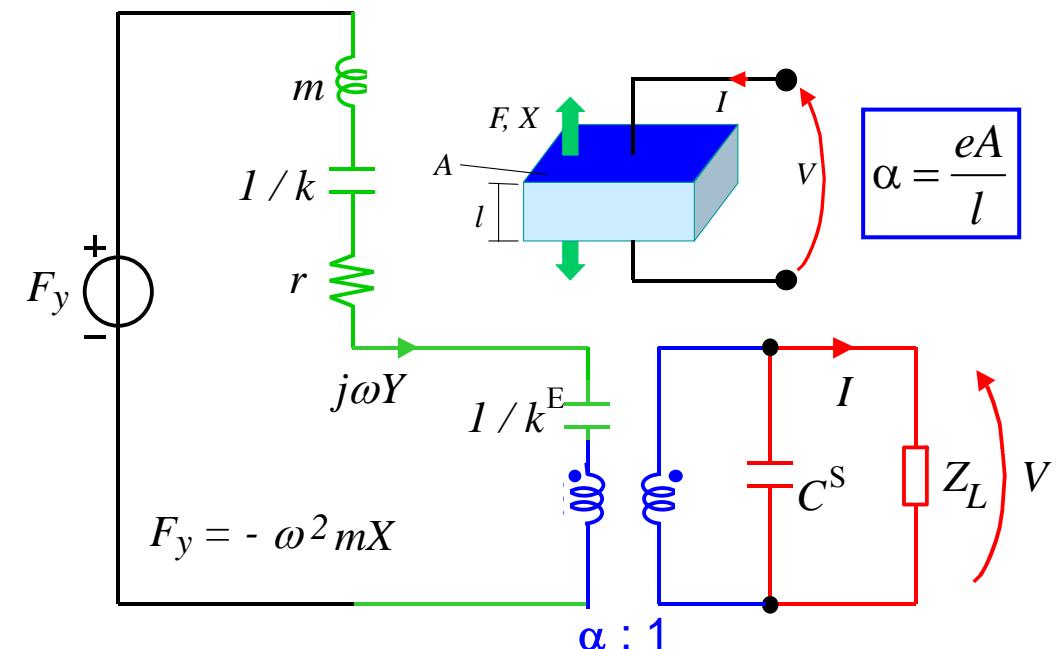
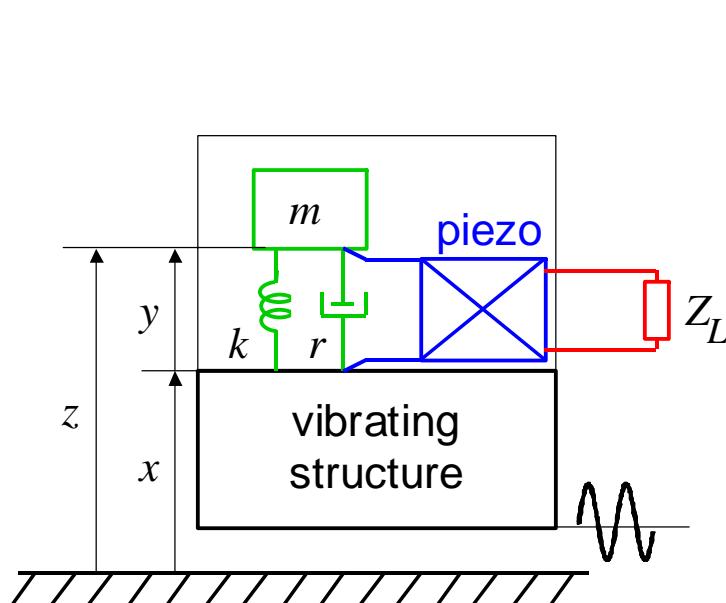
Vibration Energy Harvesting



- The load can be sensors with wireless communication:
→ **Autonomous Sensors**
- If available power is insufficient
for continuous operation
→ **Intermittent operation**



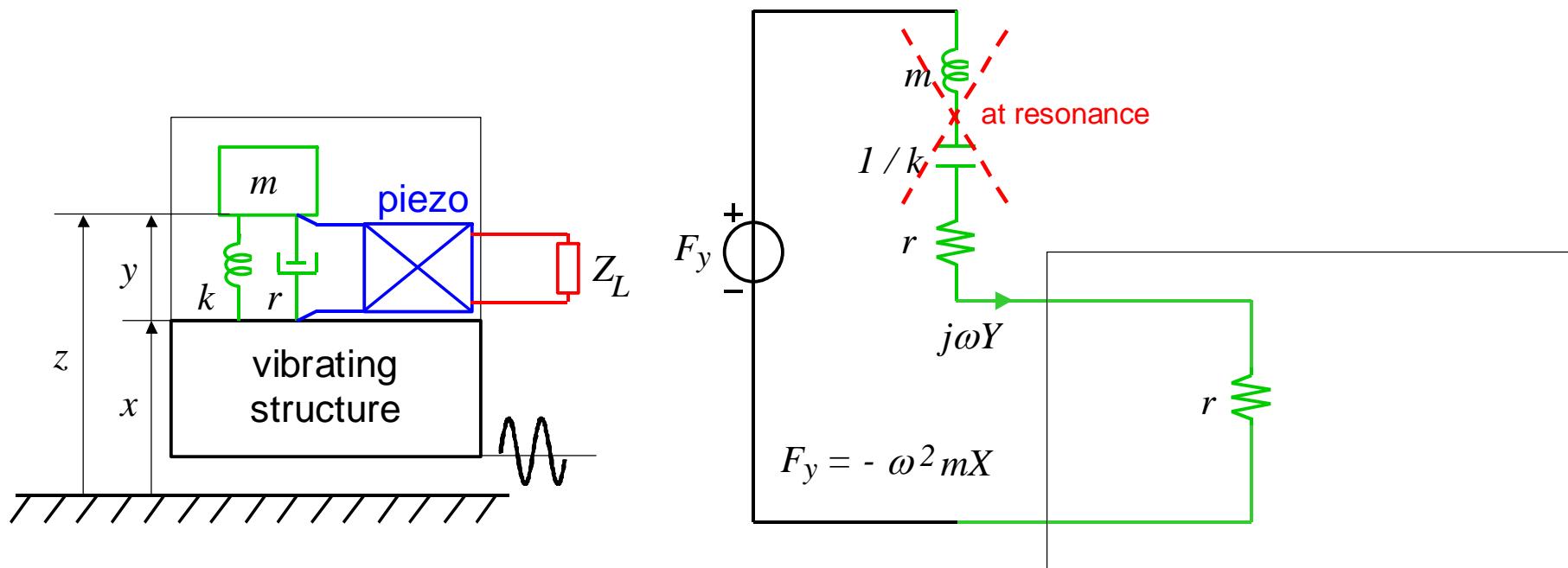
Piezoelectric Power Conversion



- A maximum exists to the power that can be extracted by an ideal converter, irrespective of the conversion principle
- This power limit occurs at resonance and for a converter with a purely resistive mechanical impedance adapted to r :

$$P_{\text{lim}} = \frac{m^2 \ddot{X}^2}{8r} = \frac{m^2 a_x^2}{8r}$$

Piezoelectric Power Conversion



- A maximum exists to the power that can be extracted by an ideal converter, irrespective of the conversion principle
- This power limit occurs at resonance and for a converter with a purely resistive mechanical impedance adapted to r :

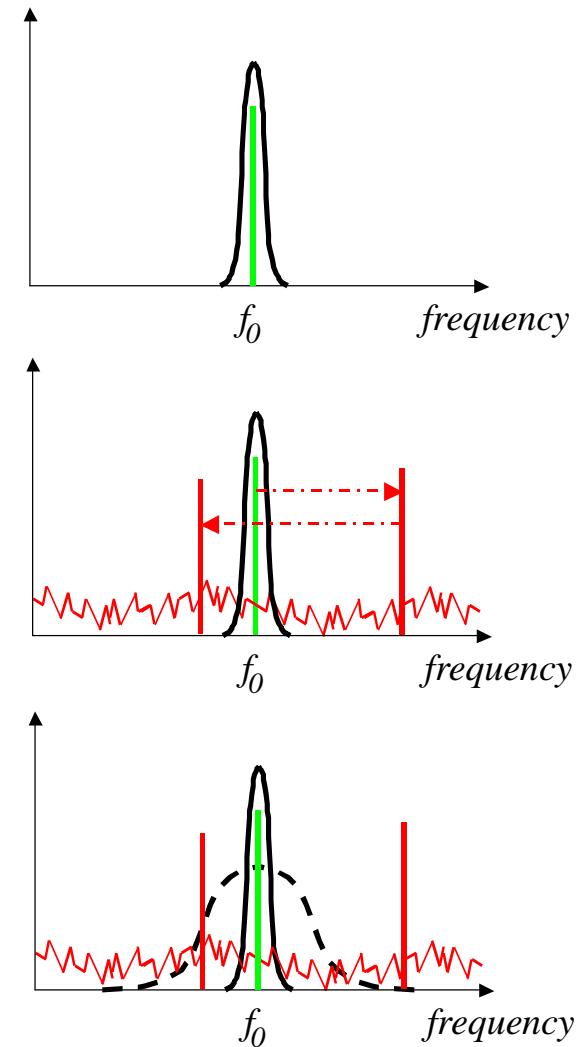
$$P_{\text{lim}} = \frac{m^2 \ddot{X}^2}{8r} = \frac{m^2 a_x^2}{8r}$$

- Same results as in:
C.B. Williams, R.B. Yates,,
Sens. Actuat. A **52**, 8-11 (1996).



Limitations with Resonant Converters

- Best harvesting effectiveness is when the converter operates at mechanical resonance
- This is problematic to guarantee with frequency-varying vibrations and is considerably sub-optimal for broadband and random vibrations
- Lowering the converter quality factor increases the bandwidth, but worsens the peak response



Broadband Approaches

IOP PUBLISHING

Meas. Sci. Technol. 21 (2010) 022001 (29pp)

MEASUREMENT SCIENCE AND TECHNOLOGY

doi:10.1088/0957-0233/21/2/022001

TOPICAL REVIEW

Strategies for increasing the operating frequency range of vibration energy harvesters: a review

Dibin Zhu, Michael J Tudor and Stephen P Beeby

School of Electronics and Computer Science, University of Southampton, SO17 1BJ, UK

Toward Broadband Vibration-based Energy Harvesting

LINHUA TANG, YADWEN YANG* AND CHIEE KHOONG SONG

School of Civil and Environmental Engineering, Nanyang Technological University, 50 Nanyang Avenue, Singapore 639798

JOURNAL OF INTELLIGENT MATERIAL SYSTEMS AND STRUCTURES, Vol. 21—December 2010

- Resonance tuning
- Multi-modal/multi-frequency harvesters
- Frequency-up conversion
- Nonlinear



V.Ferrari

London, March 28, 2012



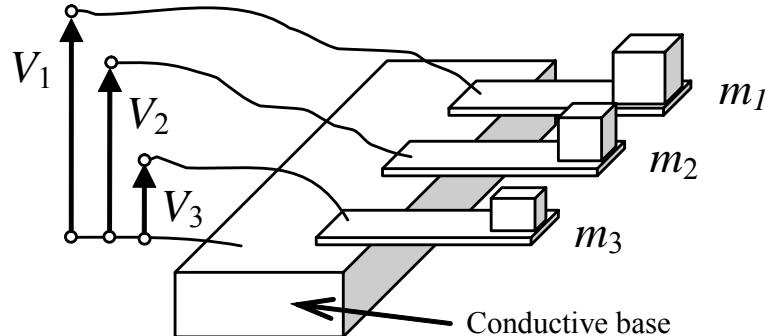
Contents

- Introduction
- Multi-frequency piezoelectric harvester arrays
- Nonlinear piezoelectric harvesters
- Conclusions

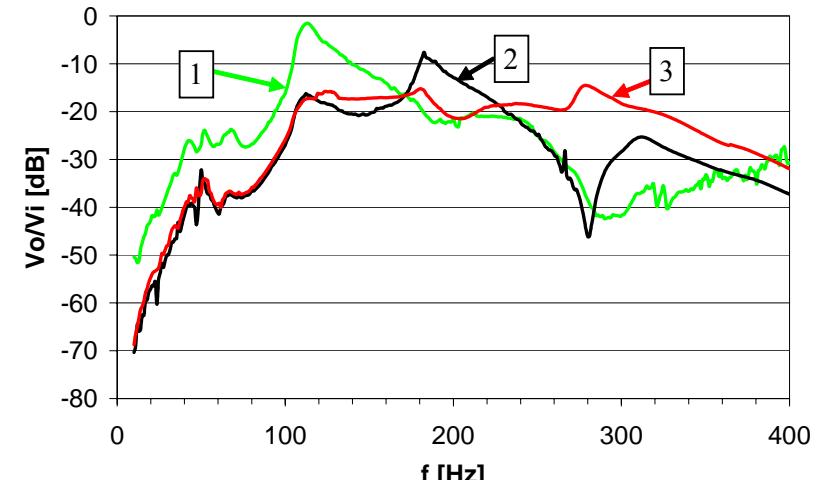
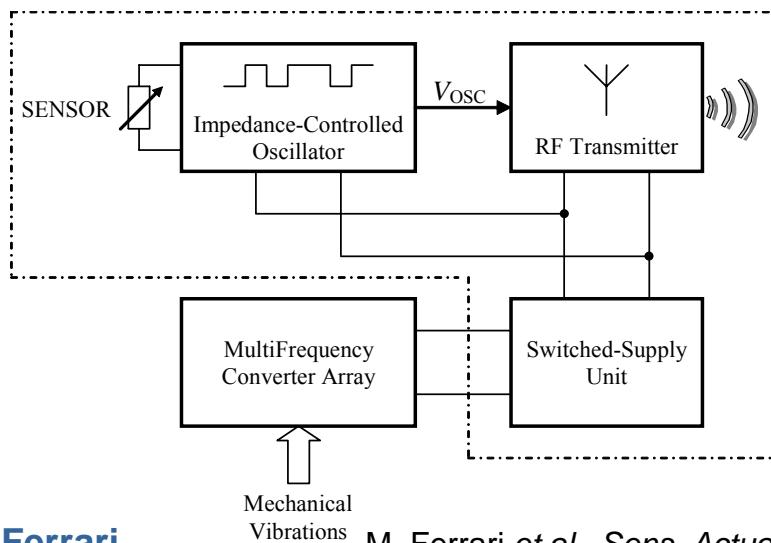


Multi-Frequency Converter Array

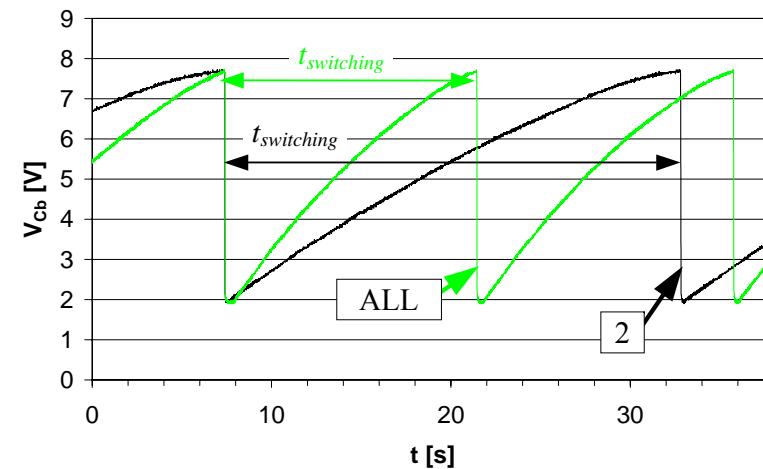
- Multiple differently-tuned converters combined to obtain a wider equivalent bandwidth:



- Bimorph commercial cantilevers (RS 285-784):
15 mm × 1.5 mm × 0.6 mm,
 $m_1 = 1.4 \text{ g}$, $m_2 = 0.7 \text{ g}$, $m_3 = 0.6 \text{ g}$.



Measured frequency response.



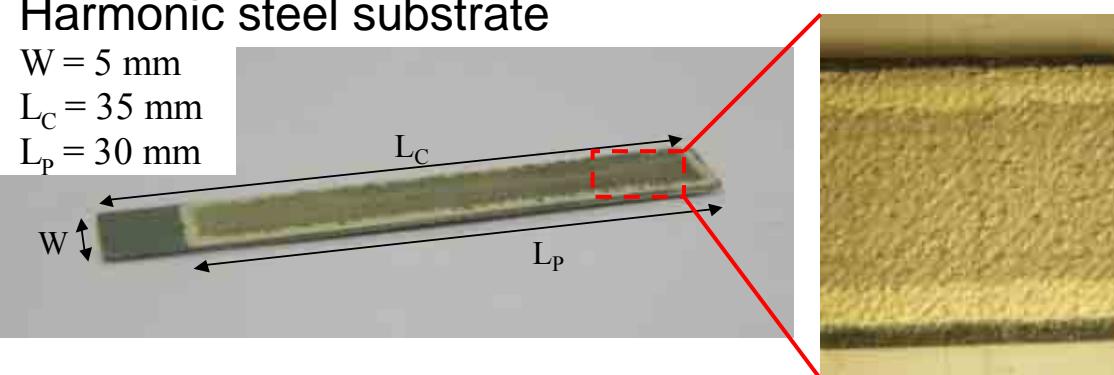
Measured voltage across the storage capacitor.

Screen-Printed Piezoelectric Films

- ◆ Lead zirconate titanate (PZT) powder in polymeric binder
- ◆ Curing: (10 min @ 150°C)
- ◆ Electrodes: Ag polymeric ink
- ◆ Poling: (10 min @ 4 MV/m @130°C)

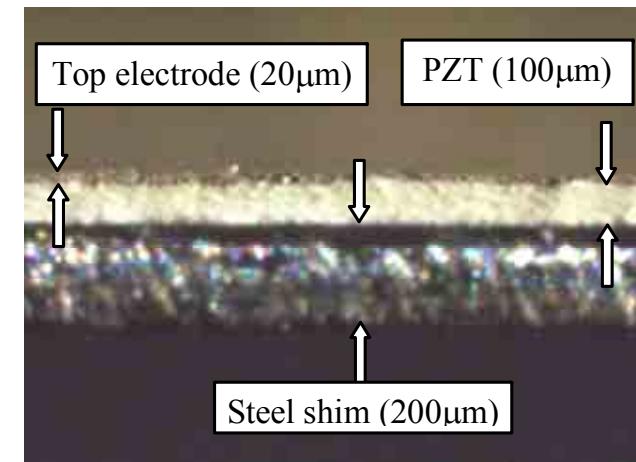
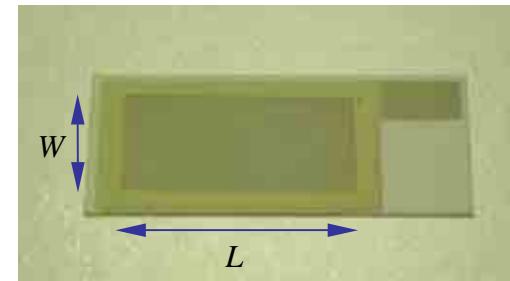
Harmonic steel substrate

$W = 5 \text{ mm}$
 $L_C = 35 \text{ mm}$
 $L_P = 30 \text{ mm}$



Alumina substrate

$W = 18 \text{ mm}$
 $L = 31 \text{ mm}$
Film Thickness
 $= 125 \mu\text{m}$



parameter

rel. permittivity ϵ^T/ϵ_0

BULK CERAMIC

4100

THICK FILM

100

density $\rho [\text{g}/\text{cm}^3]$

7.5

4.5

piezoelectric coeff. $d_{33} [\text{pC}/\text{N}]$

590

< 10

Piezokeramica-APC 856 powder
(soft material)



V.Ferrari

on, March 28, 2012



Steel Implementation of a MFCA

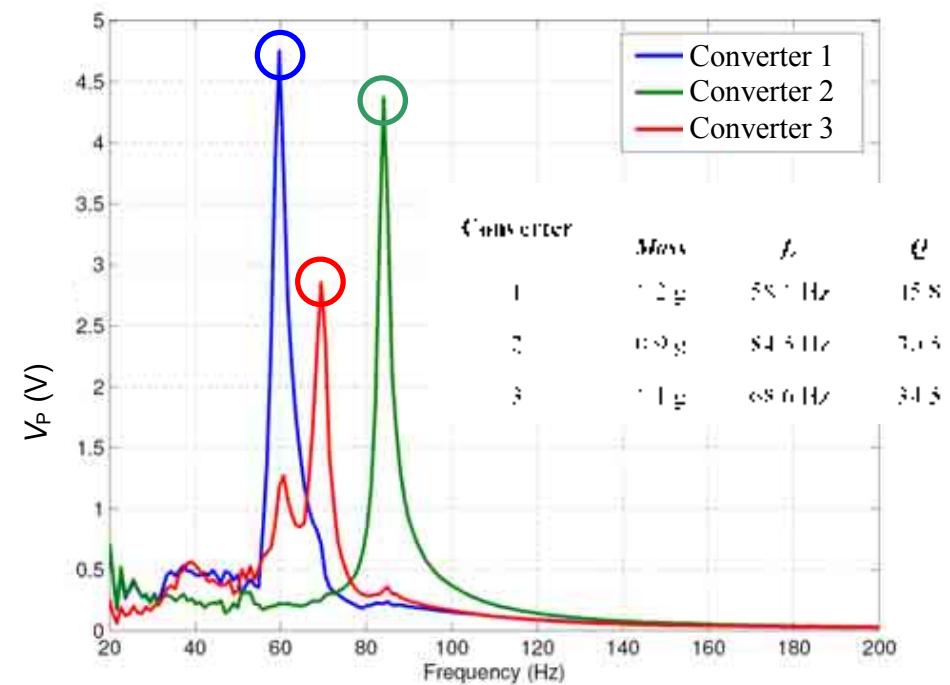
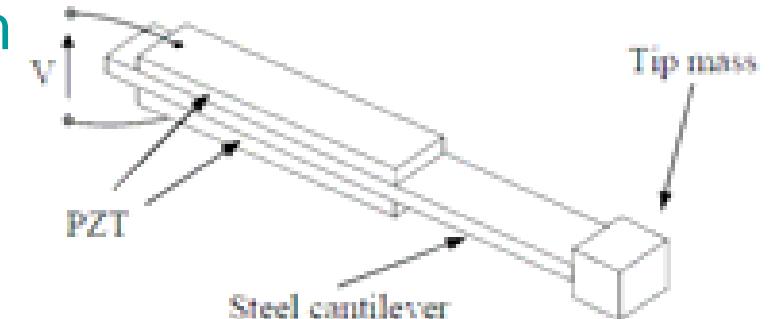
- Steel cantilevers ($40 \text{ mm} \times 5 \text{ mm} \times 0.5 \text{ mm}$)
- Cured thickness of PZT film: $75 \mu\text{m}$
- Series bimorph configuration



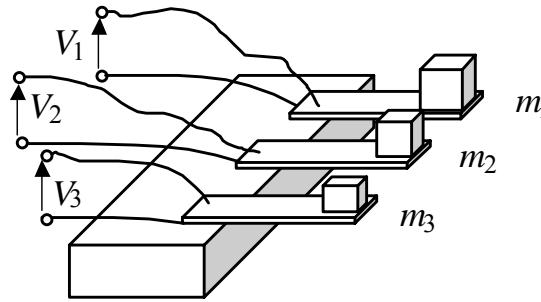
Internal impedance:

$400 \text{ pF} \parallel 20 \text{ M}\Omega @ 100 \text{ Hz}$

- Open-circuit voltages
@ 1 g_{pk} acceleration

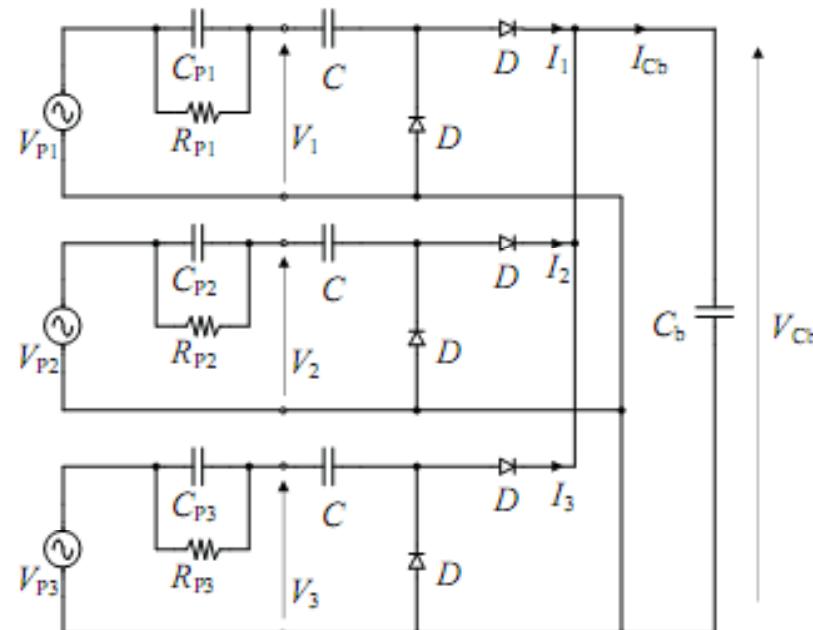


Output Combinations in a MFCA



- Parallel-like combination:

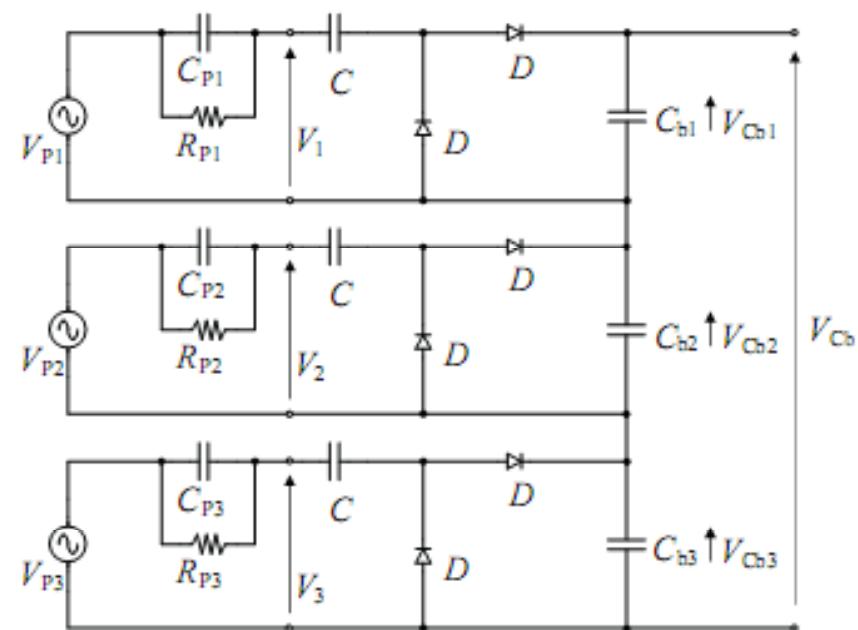
- ◆ Rectified currents are fed to a single capacitor



$$\mathbf{a)} \quad I_{C_b}(t) = I_1(t) + I_2(t) + I_3(t)$$

- Series-like combination:

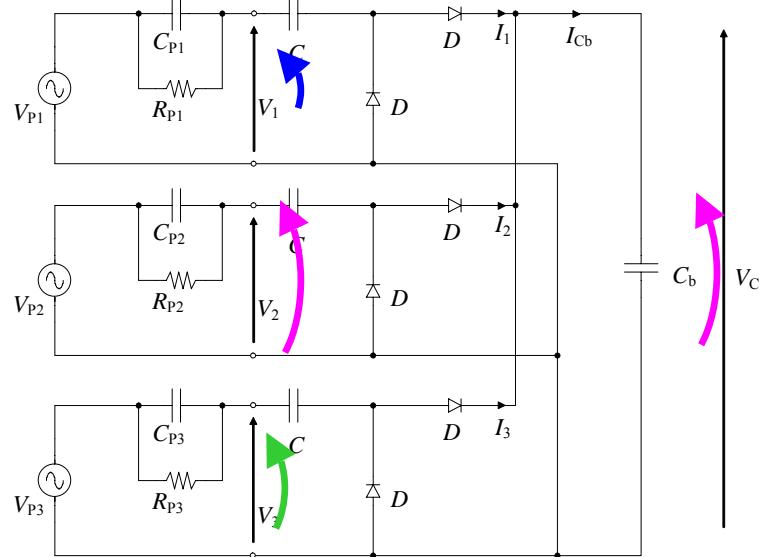
- ◆ Rectified voltages on different capacitors are summed



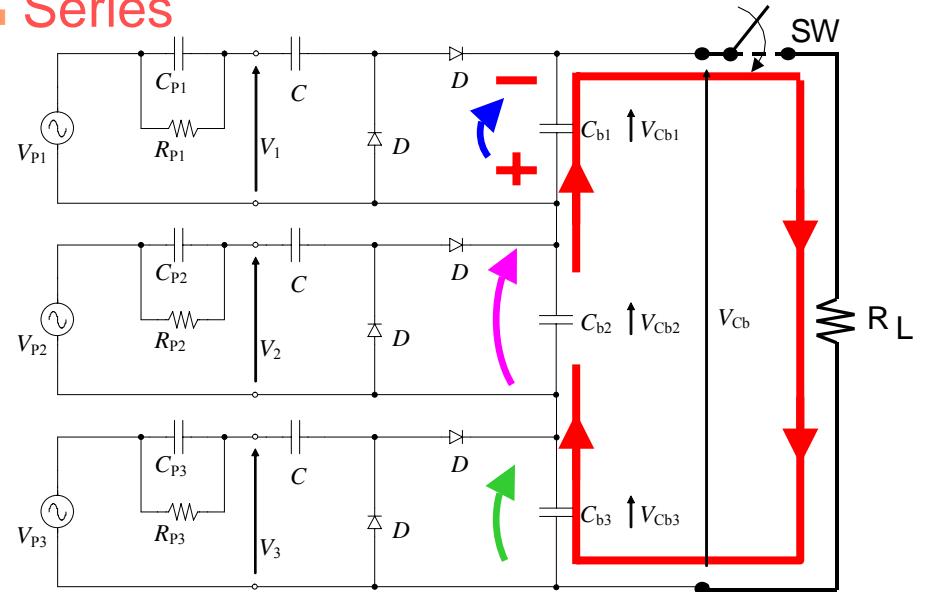
$$\mathbf{b)} \quad V_{C_b}(t) = V_{C_{b1}}(t) + V_{C_{b2}}(t) + V_{C_{b3}}(t)$$

Output Combinations in a MFCA

- Parallel



- Series

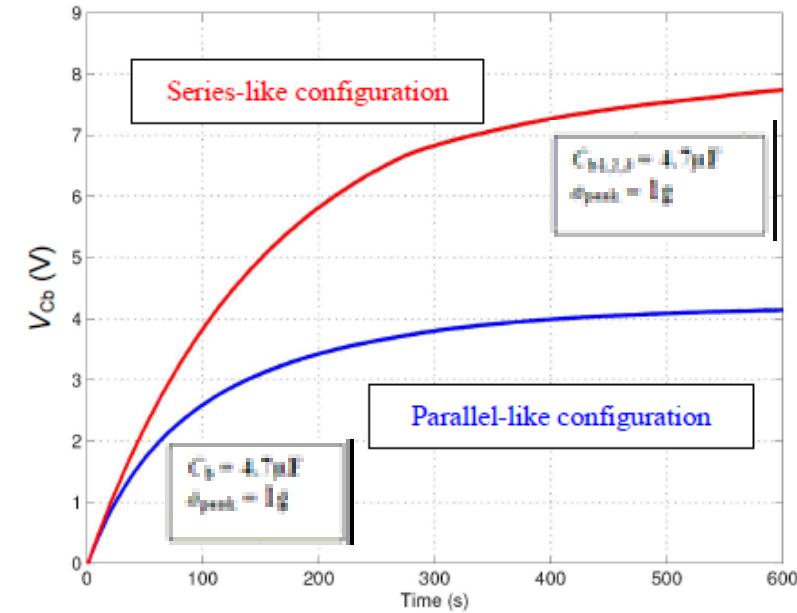
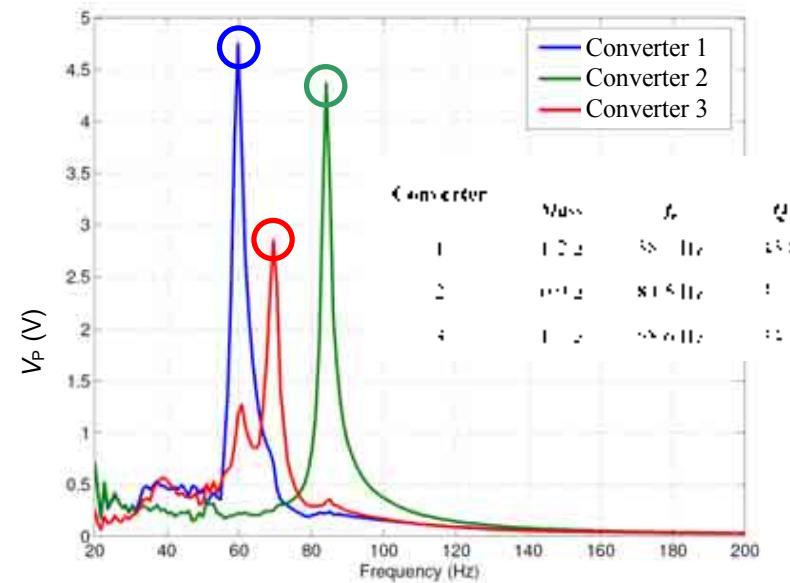


- The storage capacitor is charged prevalently by the converter with the highest instantaneous level
- The voltage is determined by the dominant converter
- Under wideband excitation, all the converters contribute to shorten the charging time

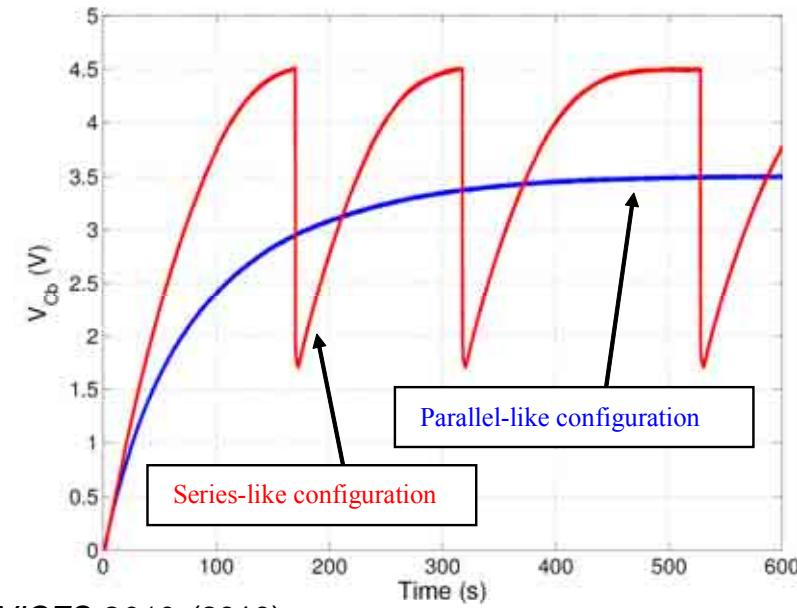
- Each storage capacitor is charged by the corresponding converter
- The voltage is given by the sum of the single voltages
- Inactive converters worsen energy transfer to the load due to charge redistribution upon switching



Experimental Results on Steel MFCA

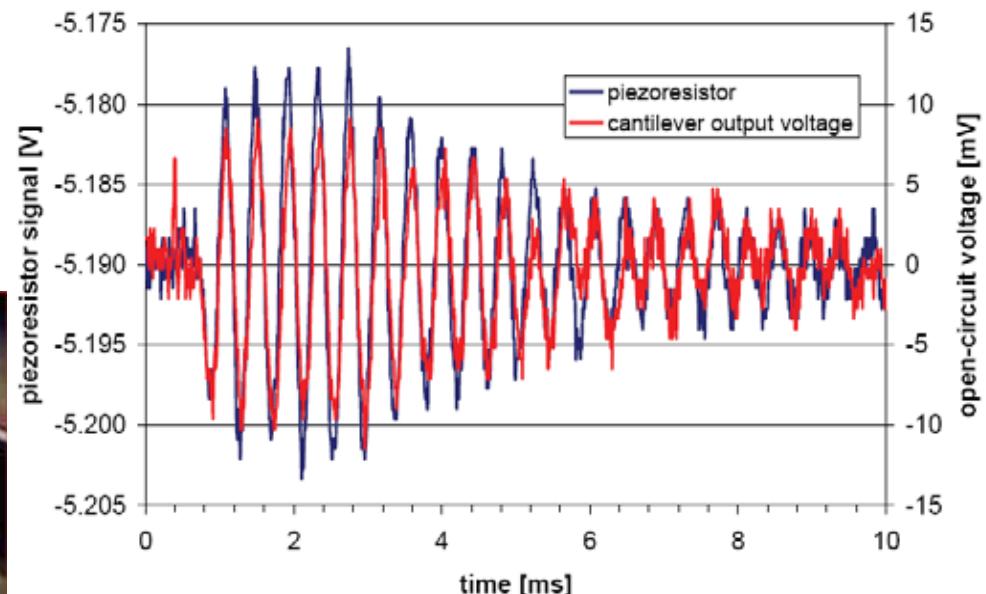
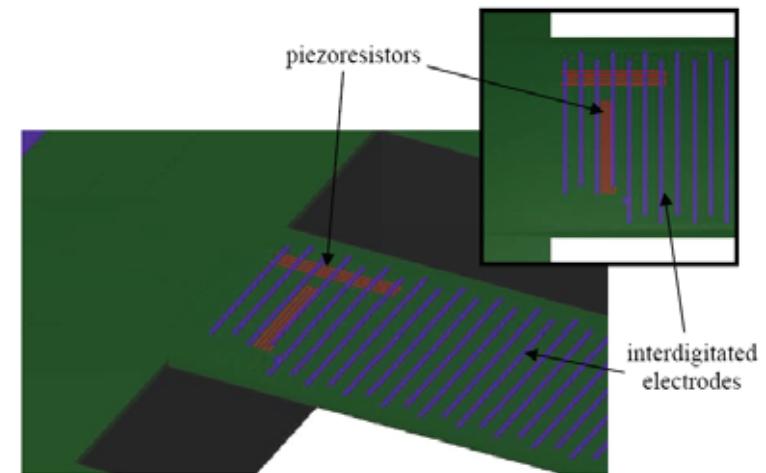
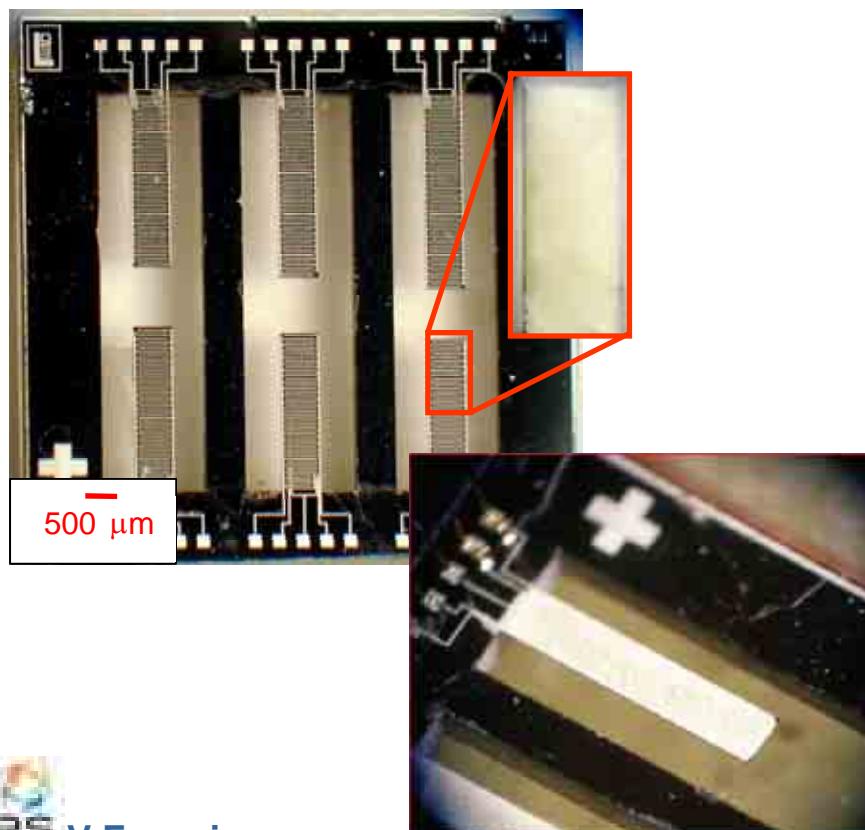


- The **series-like** configuration outputs a higher voltage at parity of excitation
- The **series-like** configuration reaches the threshold to trigger the RF transmission



MEMS Implementation of a MFCA

- Design: University of Brescia
- Fabrication: CNM, Barcelona
- PZT paste: MEGGIT/Ferroperm
- Screen-printed PZT film
- IDT electrodes (d_{33} mode)



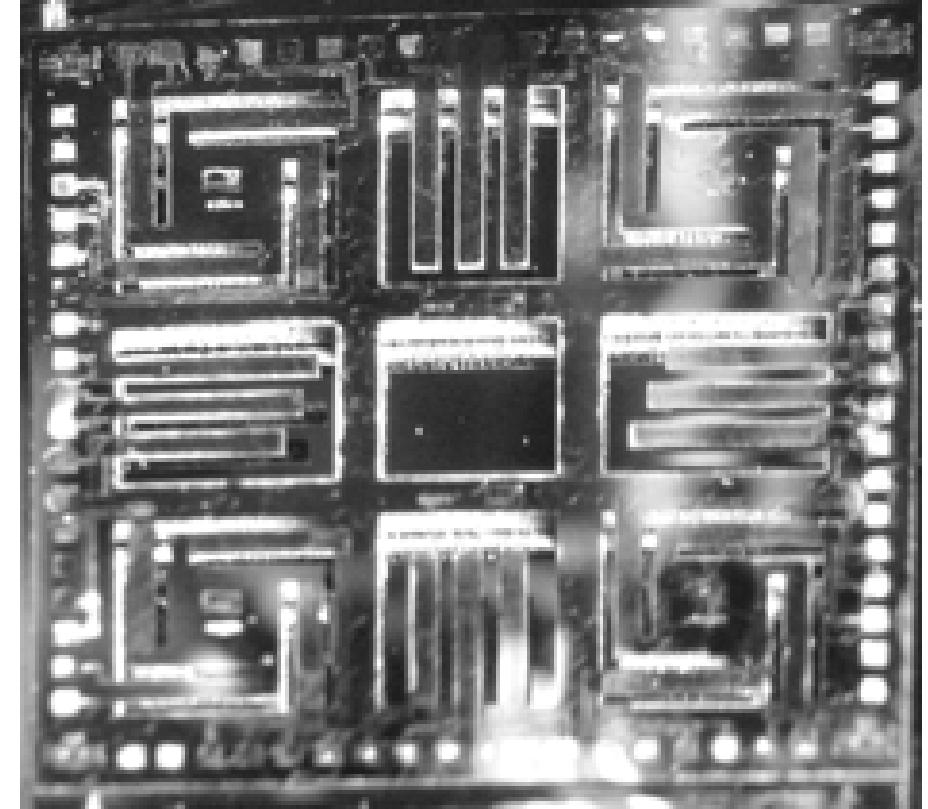
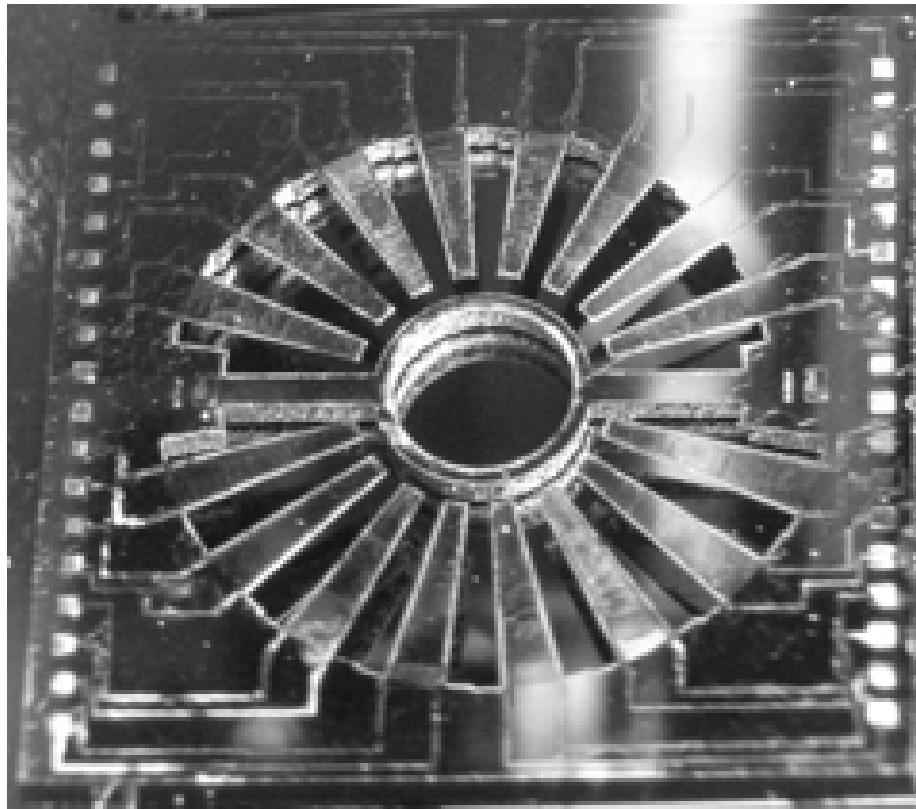
V.Ferrari

London, March 28, 2012



New Designs of MEMS MFCAs

- Array of straight and tapered cantilevers
- Design: University of Brescia
- Fabrication: CNM, Barcelona
 - ◆ BE-SOI process (10 mm × 10 mm) die
 - ◆ Cantilever resonant frequencies: 4.5÷9 kHz - 3.5÷6.5 kHz



V.Ferrari

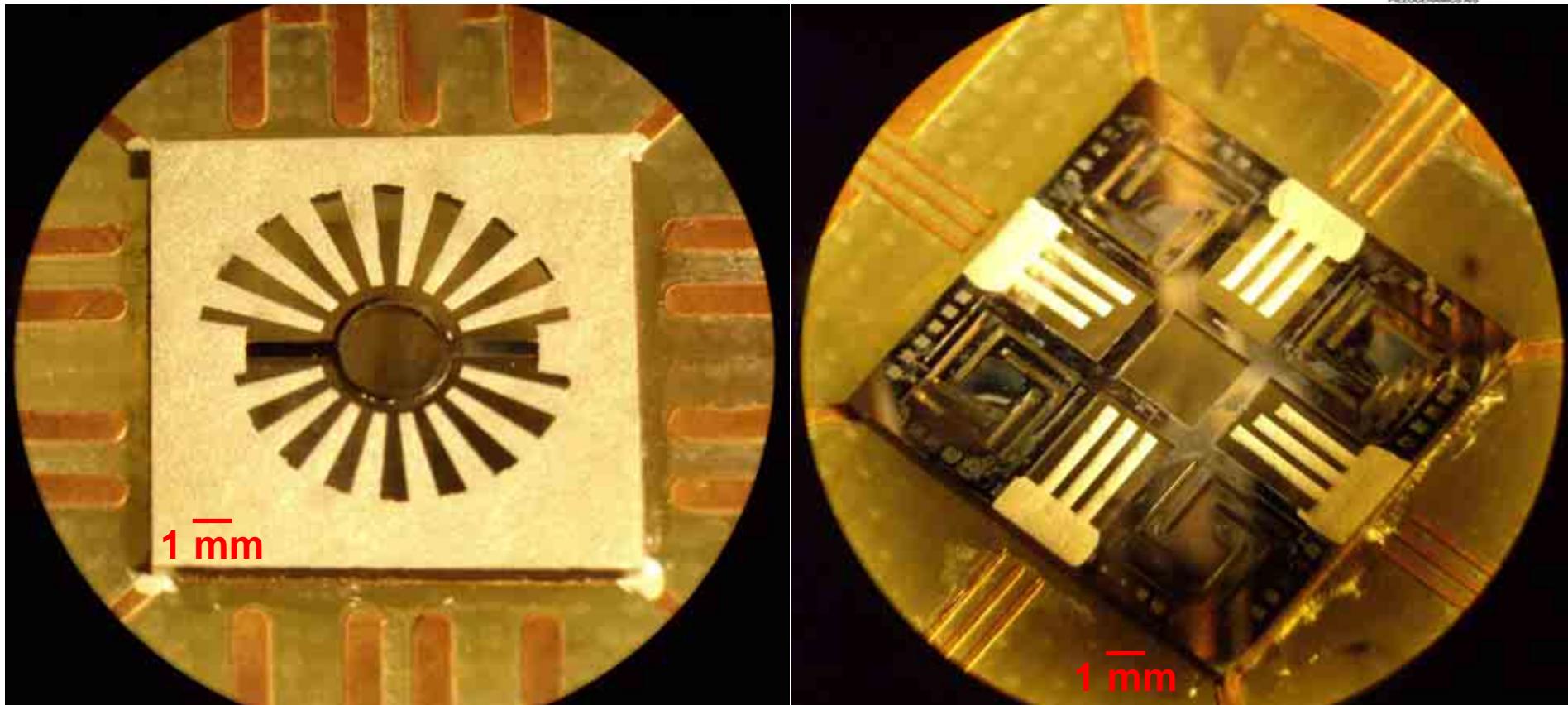
London, March 28, 2012



Deposition of Piezoelectric Film

- Sputtered Cr bottom electrode ($t_{Cr} \approx 0.5 \mu m$)
- Screen-printed PZT film ($t_{PZT} \approx 30 \mu m$)
 - ◆ PZT paste: MEGGIT/Ferroperm

MEGGITT
FERROPERM
PIEZOCERAMICS A/S



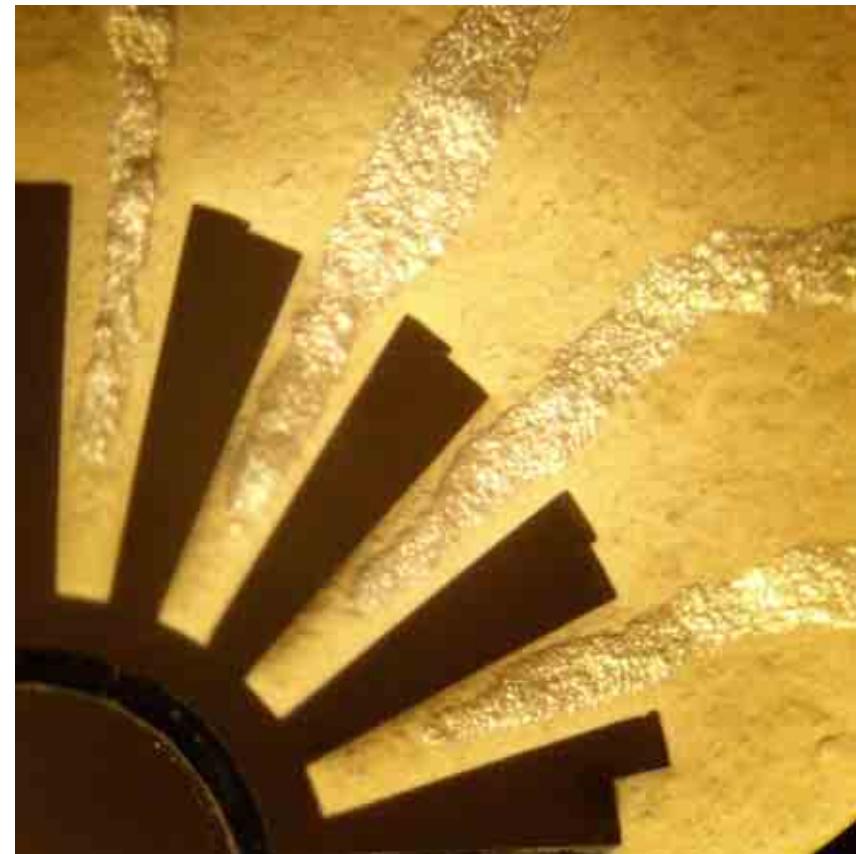
V.Ferrari

London, March 28, 2012



Top Electrode and Poling

- Top electrode: direct writing* of Ag polymeric ink
- Poling: 120 V @100°C, 10 min



* Manual artwork in the first prototype



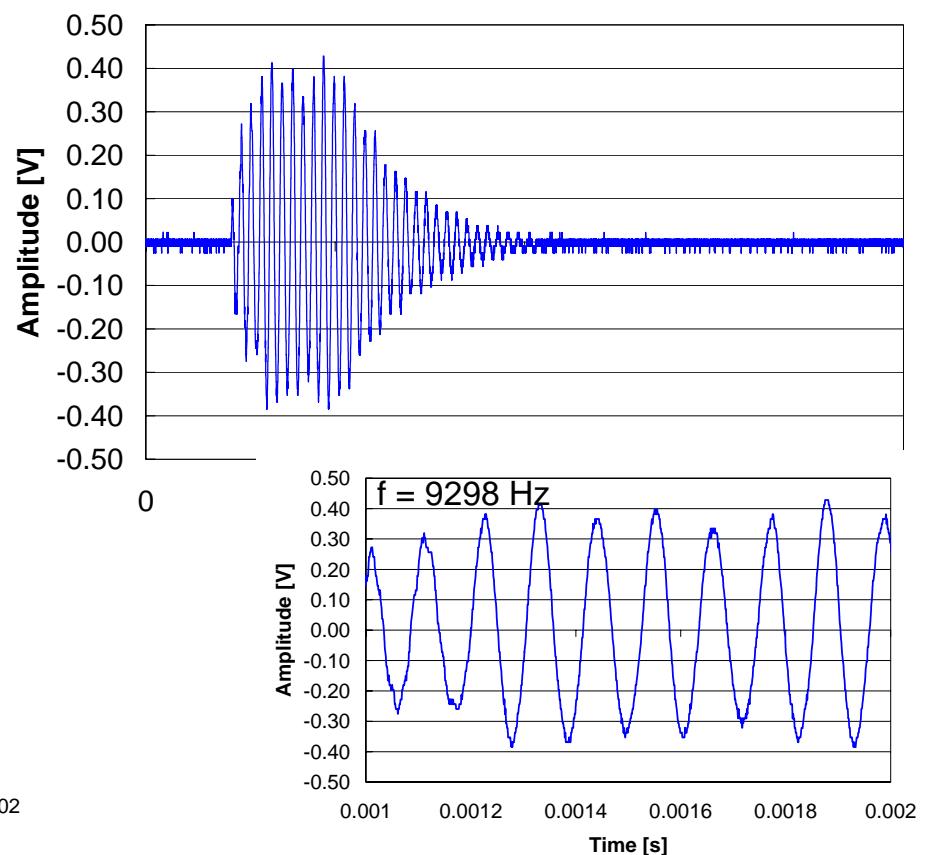
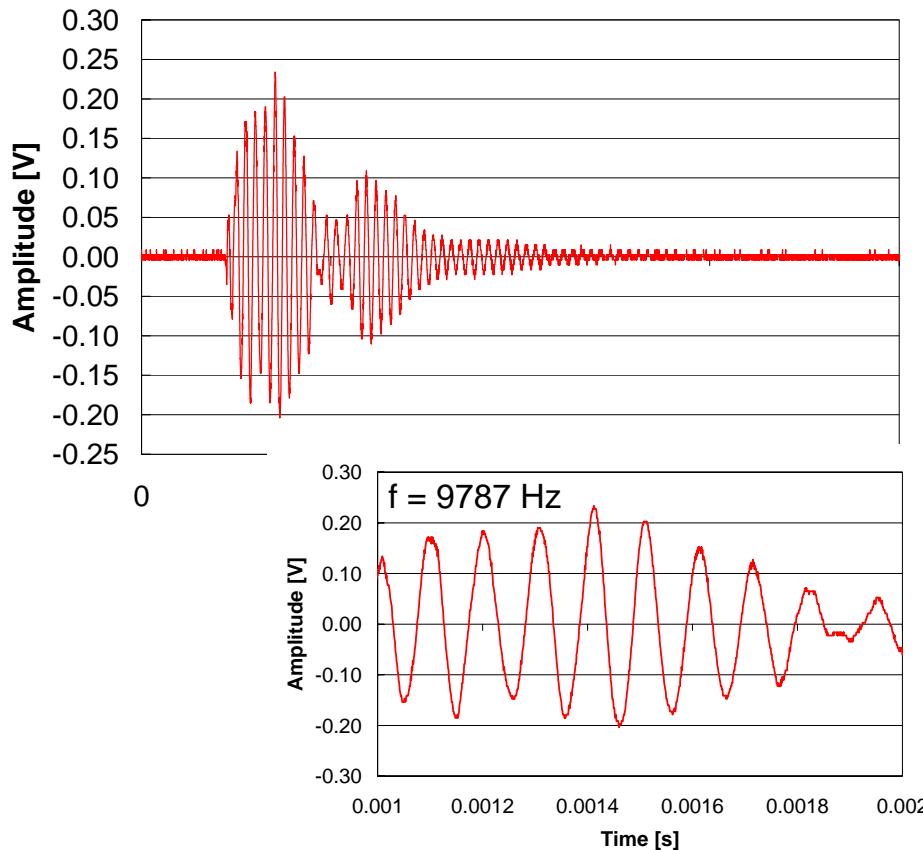
V.Ferrari

London, March 28, 2012

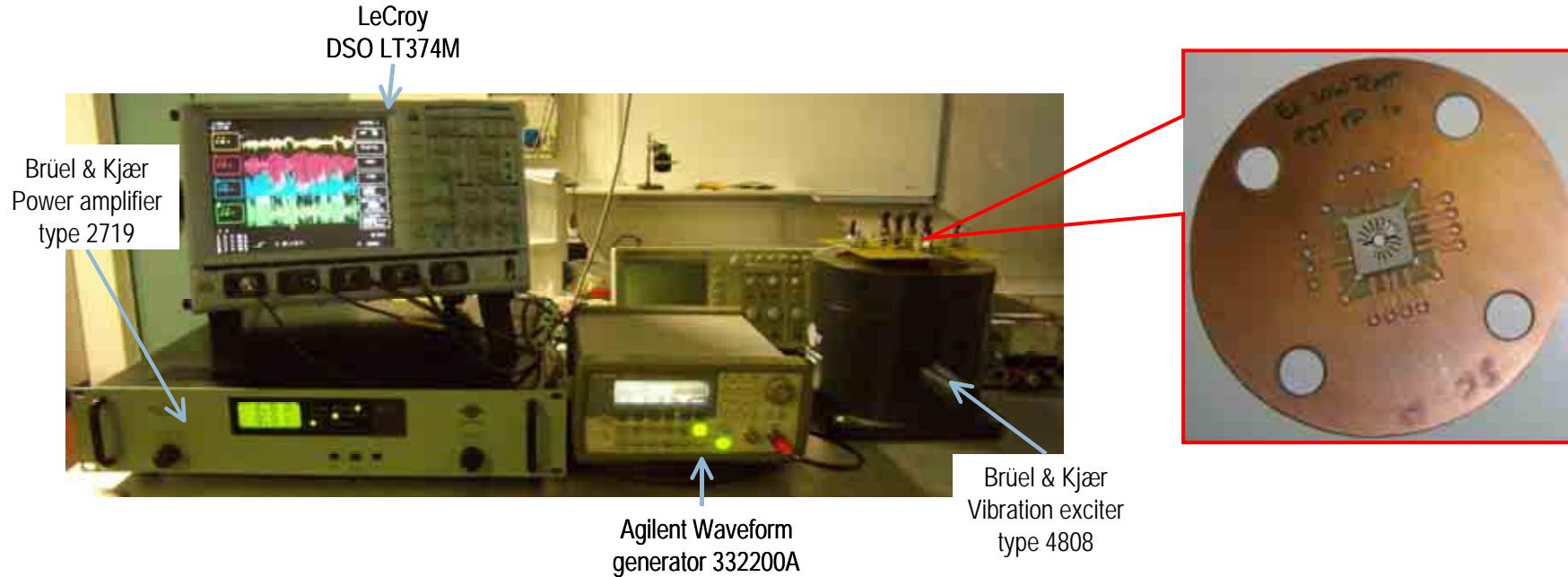


Preliminary Results

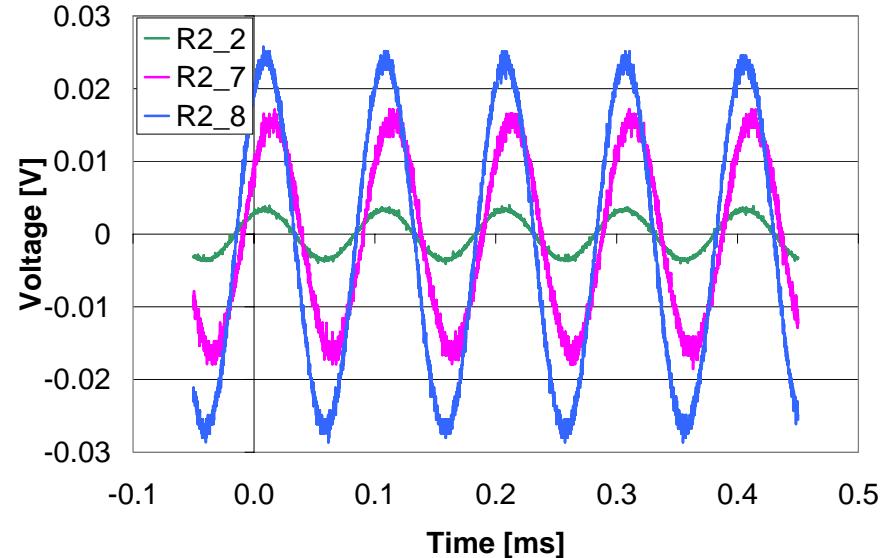
- Internal impedance @ 10 kHz:
 - ◆ $C_P = 7 \div 10 \text{ pF}$; $R_P = 10 \div 30 \text{ M}\Omega$
- Impulse response tests:



Preliminary Results



- Sinusoidal excitation of the shaker ($a_{pk} \approx 1 g$)
- Measurement of open-circuit voltage



Contents

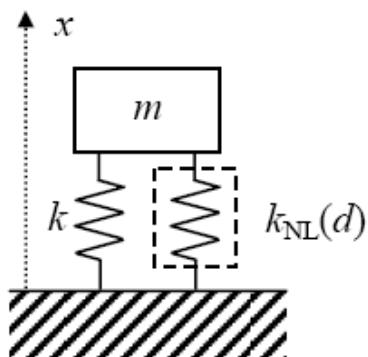
- Introduction
- Multi-frequency piezoelectric harvester arrays
- **Nonlinear piezoelectric harvesters**
- Conclusions



Nonlinear Converter

Collaboration with Univ. Catania (**S. Baglio**) and Univ. Perugia (**L. Gammaitoni**)

- **Bistability** is exploited to amplify displacement induced by **broadband vibrations**
- For decreasing values of d :
 - ◆ Quasi linearity
 - ◆ Nonlinearity
 - ◆ Bistability

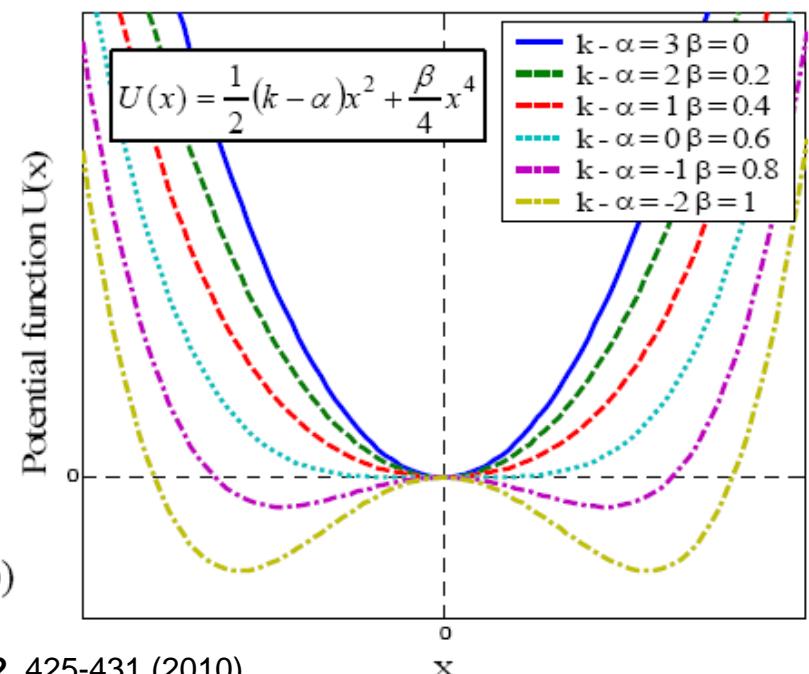
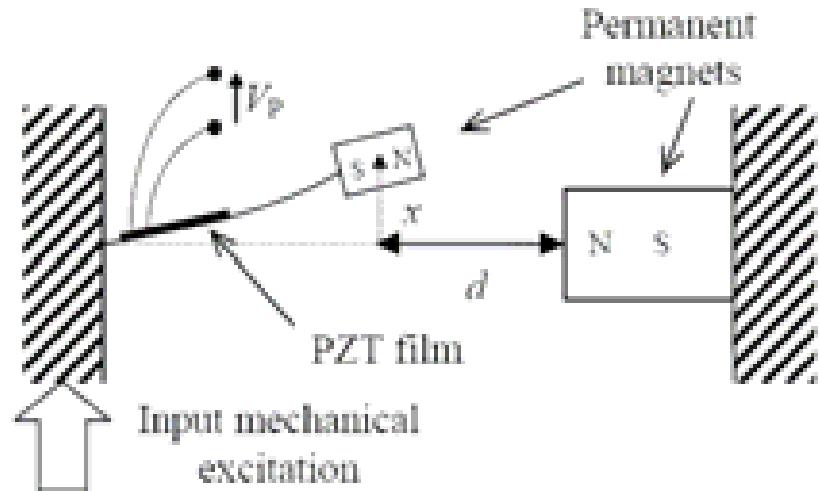


(a)

$$m\ddot{x} + (k - k_{NL})x = 0$$

$$k_{NL}(d) = \alpha - \beta x^2$$

$$F_{NL}(d) = \alpha x - \beta x^3$$

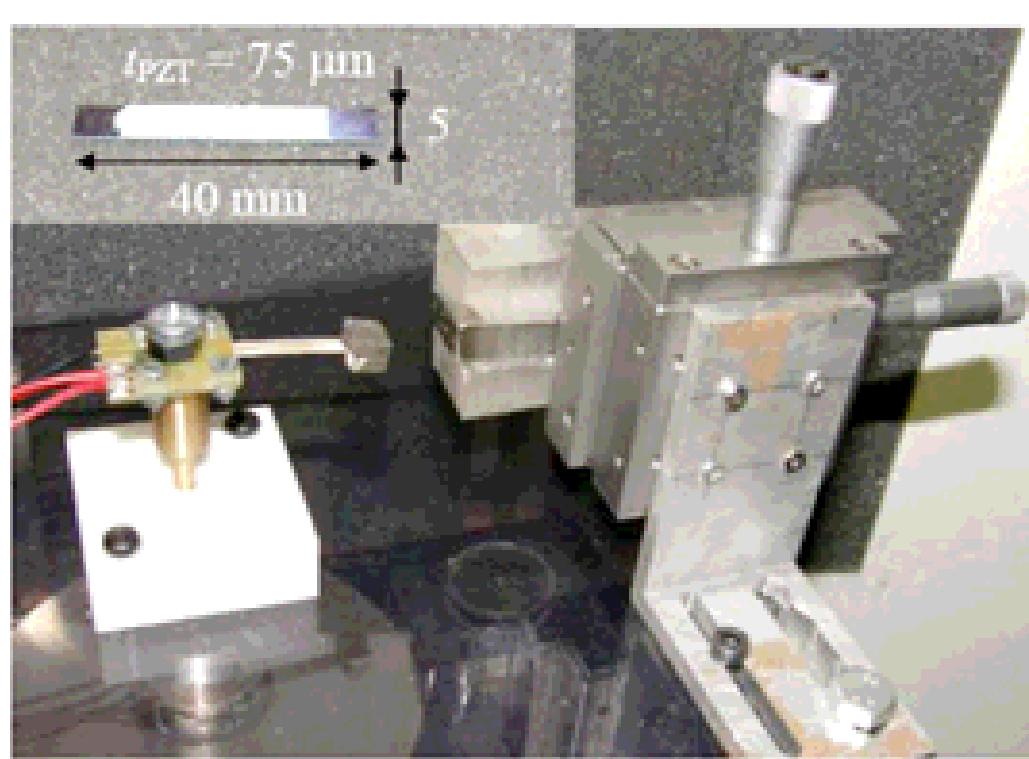


V.Ferrari

M. Ferrari *et al.*, *Sens. Actuat. A* **162**, 425-431 (2010).

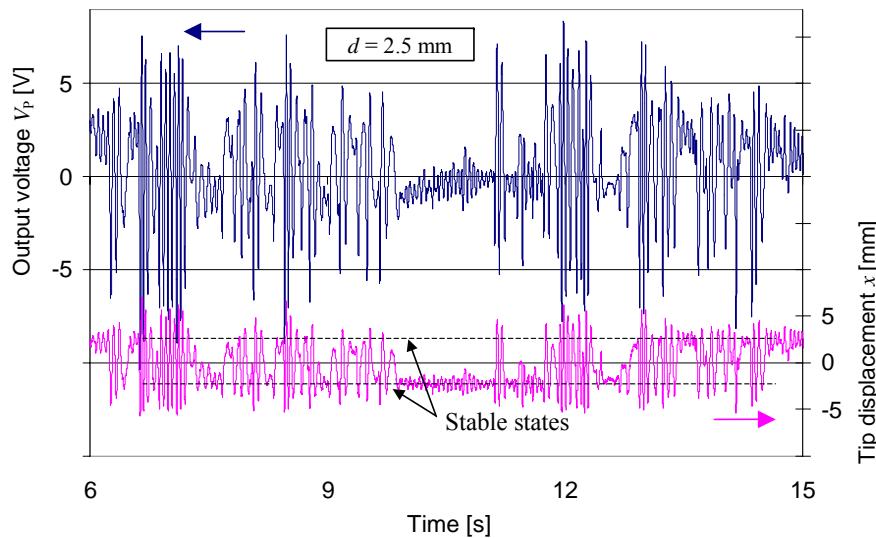
Nonlinear Converter: Experiment

- Bimorph cantilever beam fabricated with:
 - ◆ Stainless steel substrate (thickness 200 μm)
 - ◆ Low-curing-temperature PZT films
- White-noise excitation filtered in the bandwidth 1-100 Hz



Nonlinear Converter: Results

- For suitably low gap d , jumps occur between stable states
- The output voltage spectrum broadens and $V_{P\text{rms}}$ increases



$$a_{\text{rms}} = 0.3 \text{ g}$$

Distance d [mm]

25

5

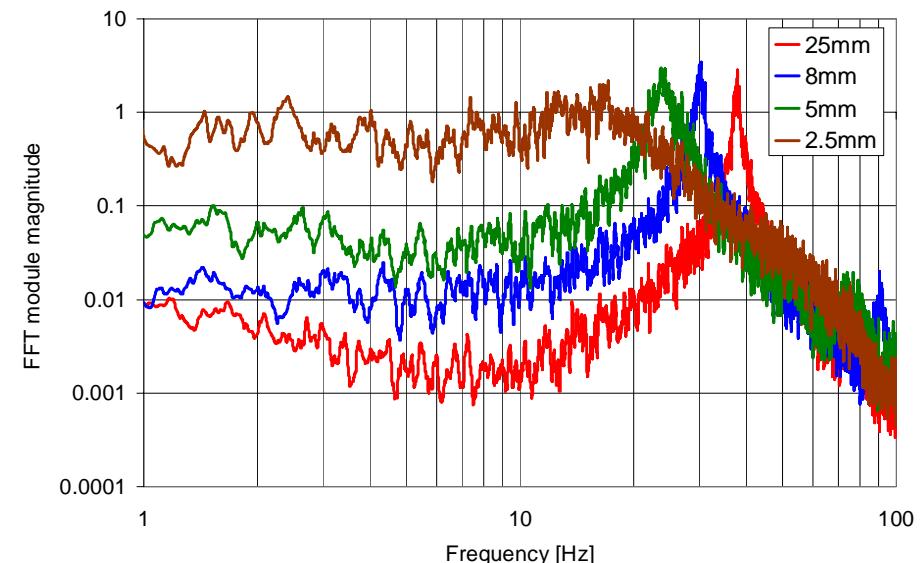
2.5

rms output voltage $V_{P\text{rms}}$ [V]

4.27

6.11

7.99

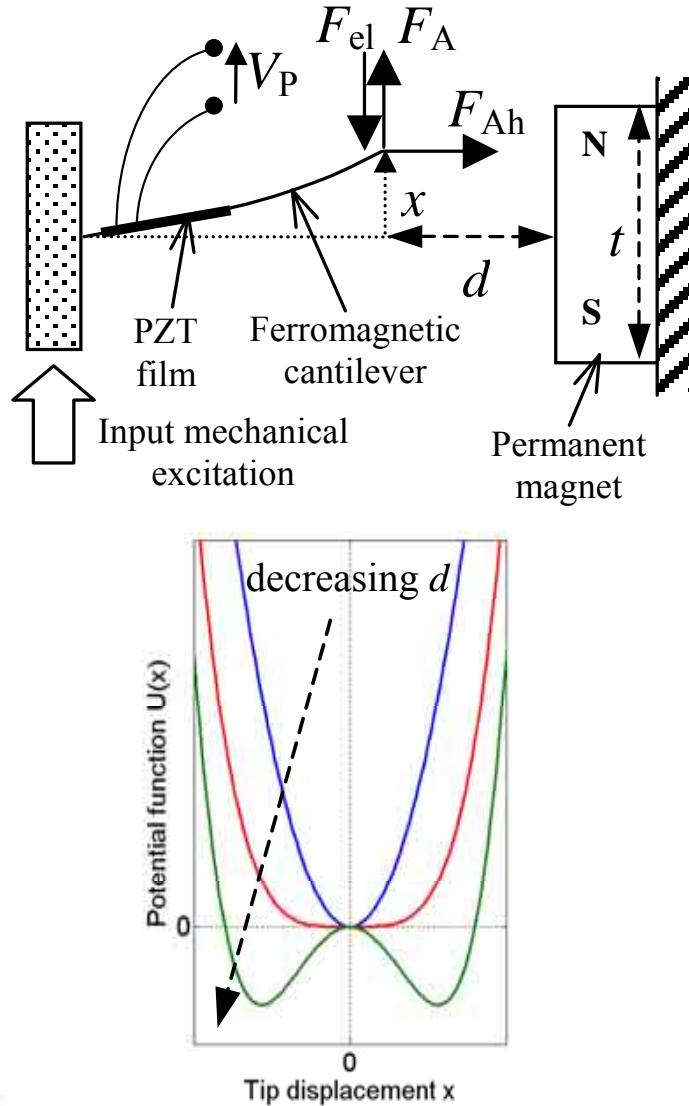


- Complex dynamics, see: S.C. Stanton *et al.*, *Physica D* **239**, 640-653 (2010).

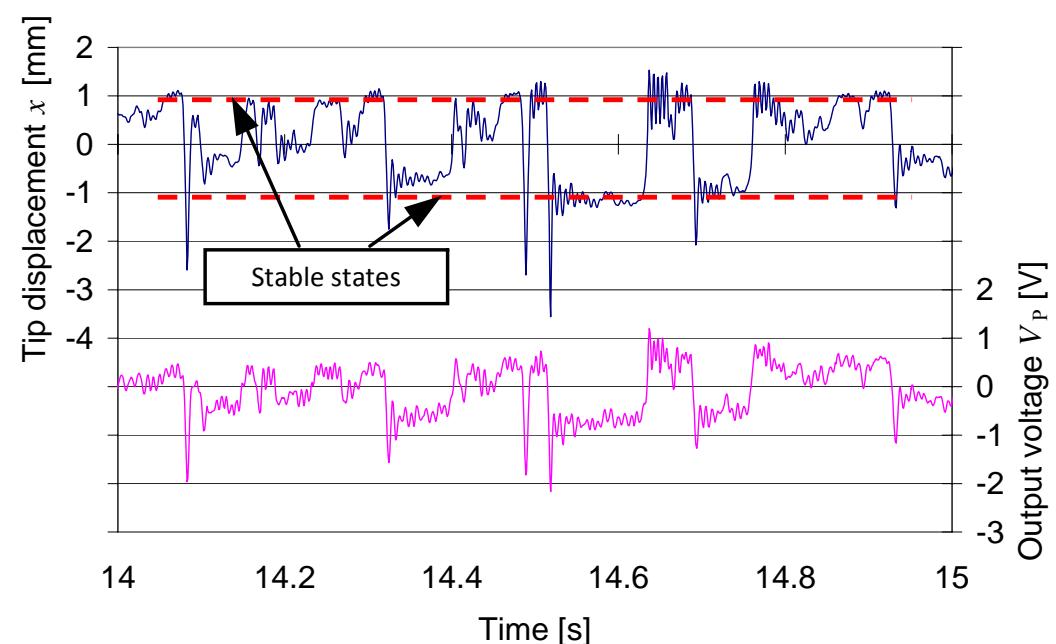


Nonlinear Single-Magnet Converter

- A ferromagnetic substrate is coupled to a fixed magnet



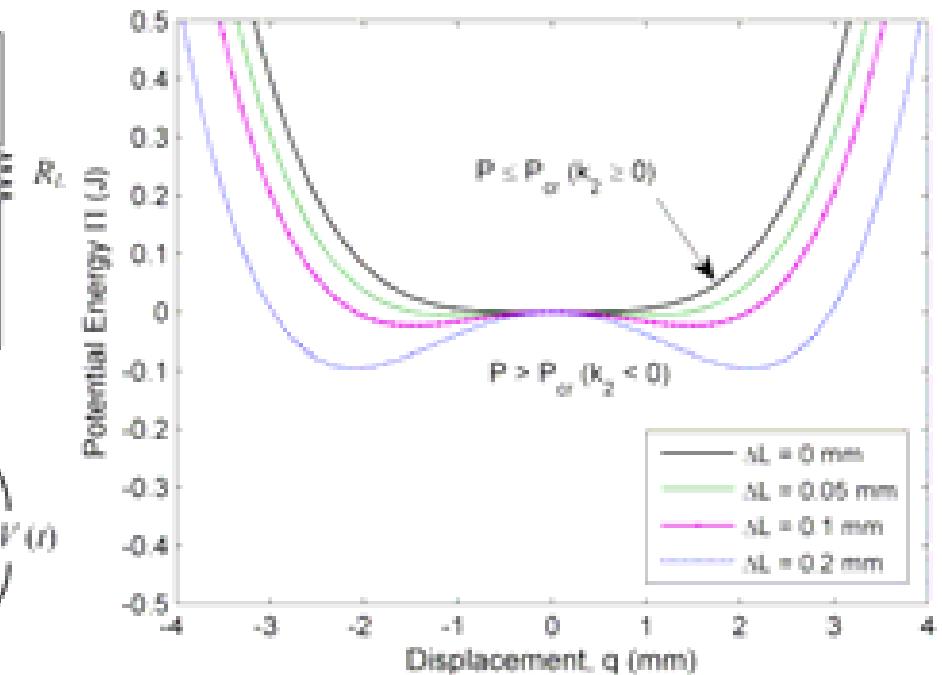
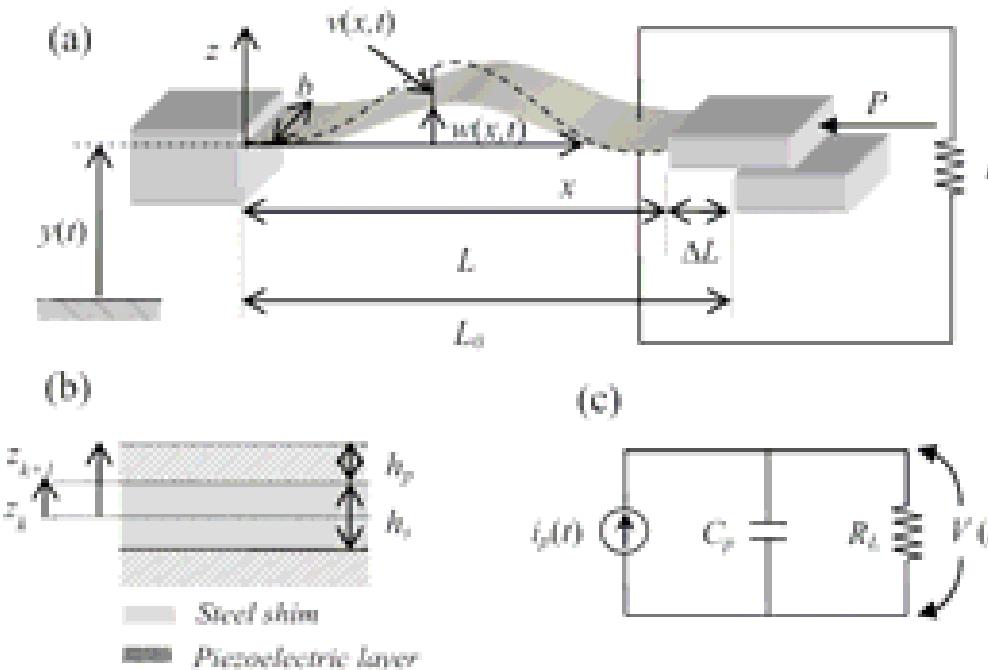
$$F_{Av} = \alpha x - \beta x^3 \quad F_{el} = -kx \quad U(x) = \frac{(k - \alpha)}{2} x^2 - \frac{\beta}{4} x^4$$



Mechanically-Induced Bistability

Collaboration with Univ. Paris-Est ([F. Cottone](#)) and Univ. Perugia ([L. Gammaitoni](#))

- An elastic beam compressed up to buckling shows bistability and double-well potential
- PZT layers on the beam perform enhanced energy conversion from bending vibrations

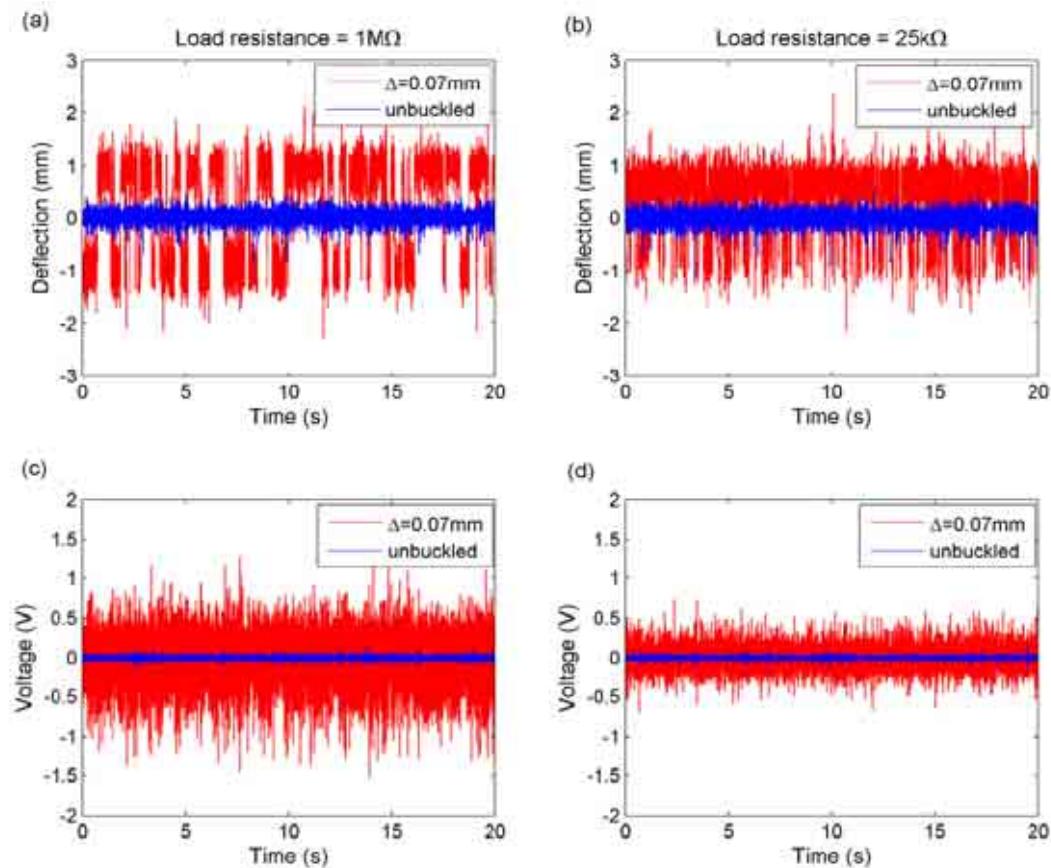
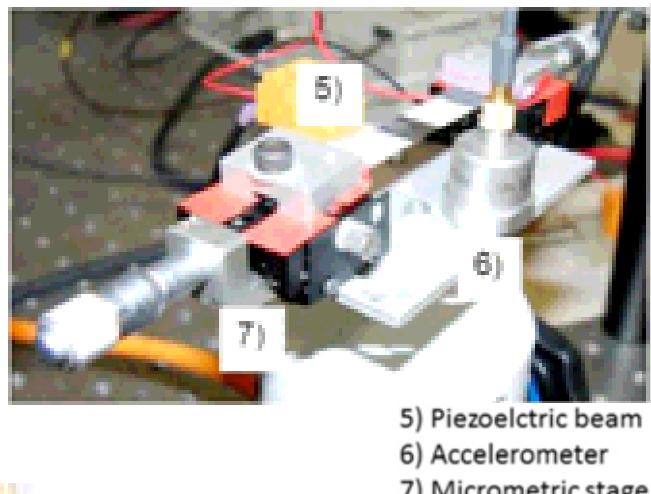


Experimental Results

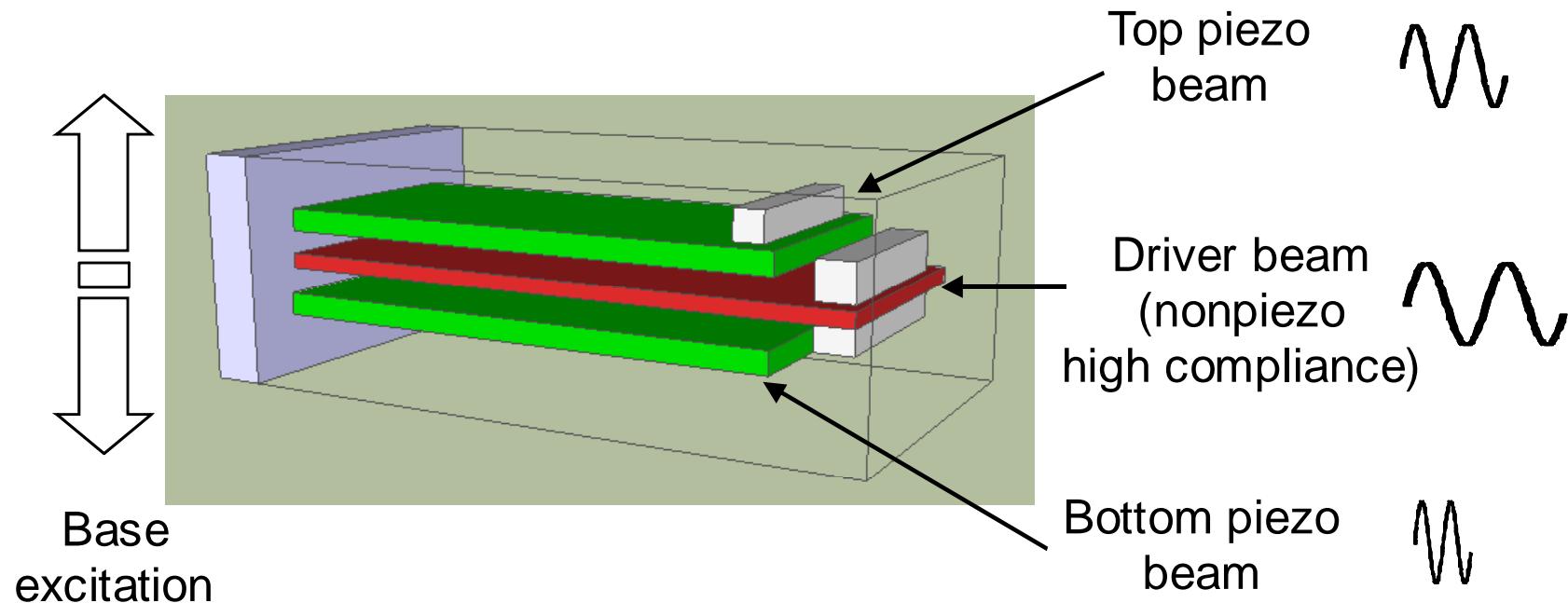
Collaboration with Univ. Paris-Est ([F. Cottone](#)) and Univ. Perugia ([L. Gammaitoni](#))

Steel shim		Piezoelectric layer	
Parameter, symbol	Value	Parameter, symbol	Value
Material	Steel	Material	PZT film
Length, L_0	55 mm	Length of layers, L_p	55 mm
Width, b	11 mm	Length of electrodes, L_e	21 mm
Thickness, h_s	0.1 mm	Width, $b_p = b$	10 mm

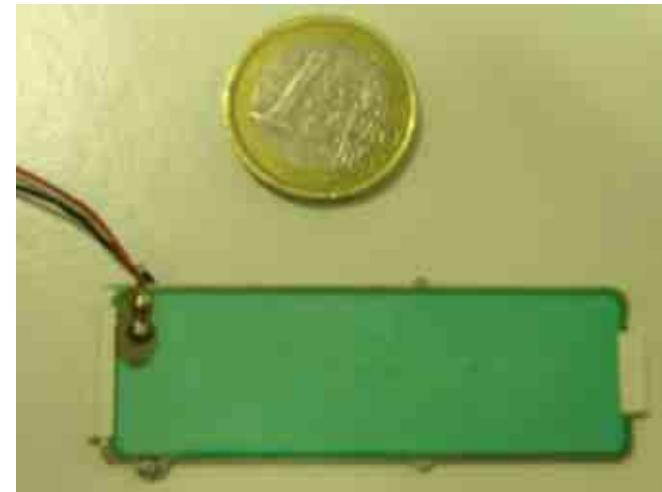
- PZT films screen printed on steel shims ($f_0 = 220$ Hz)
- Shaker driven by Gaussian noise: autocorrelation time $\tau = 1$ ms; acceleration $1 \div 3 g_{rms}$



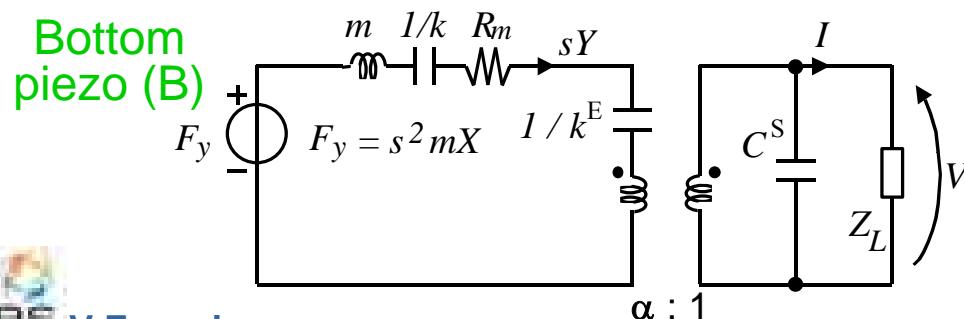
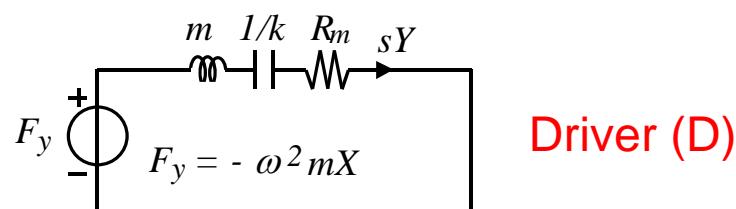
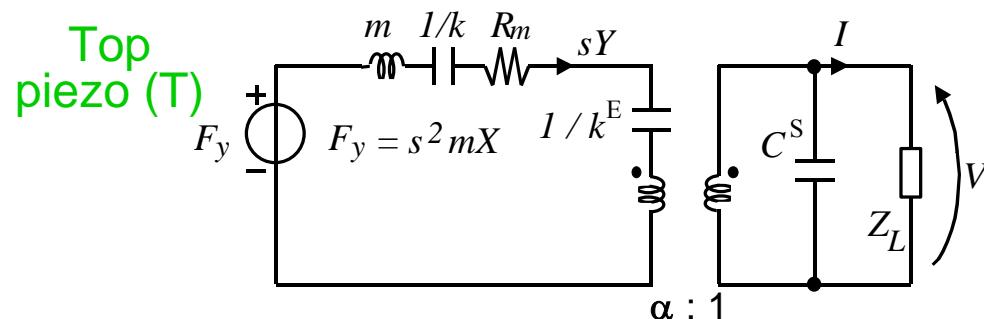
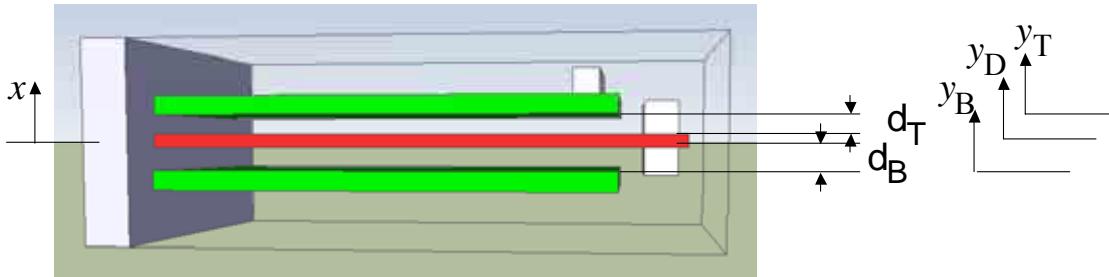
Impact-Enhanced Multi-Beam EH



- PZT parallel bimorph on flexible steel
 - ◆ Beam dimensions: $(45 \times 19 \times 0.58) \text{ mm}^3$
 - ◆ Internal impedance @ 100Hz: $C_p = 270 \text{ nF}; R_p = 20 \text{ k}\Omega$

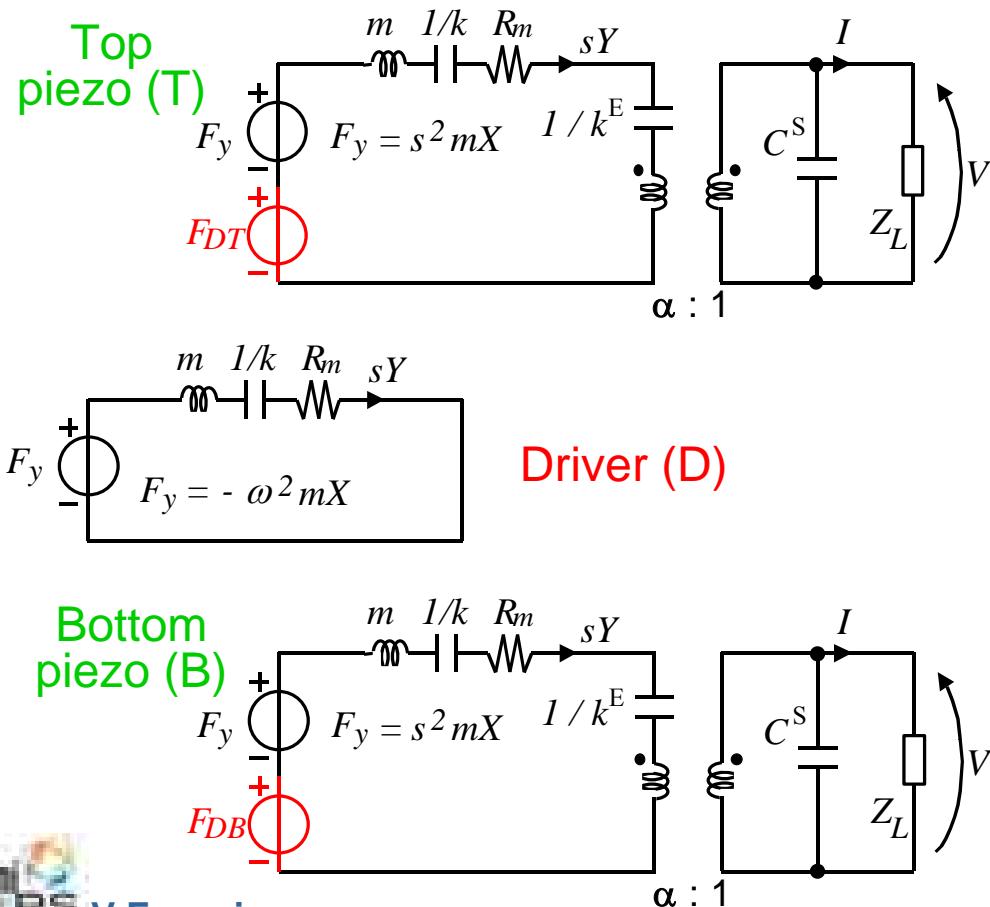
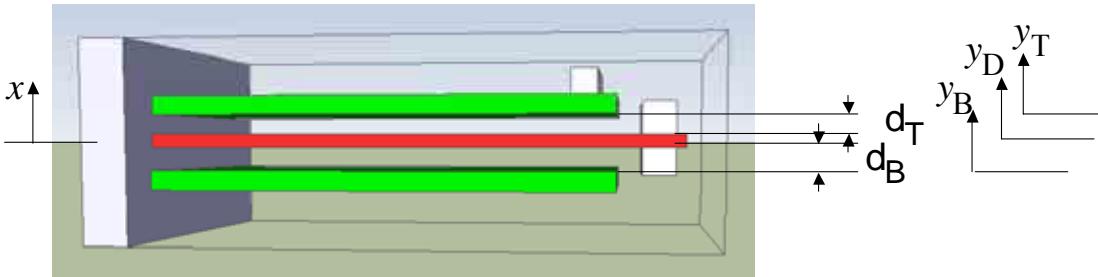


Modelling: Noninteracting Beams



- T, B and D beams operate independently as uncoupled oscillators
- The outputs of T and B peak at the respective resonant frequencies
- Poor response at low frequency

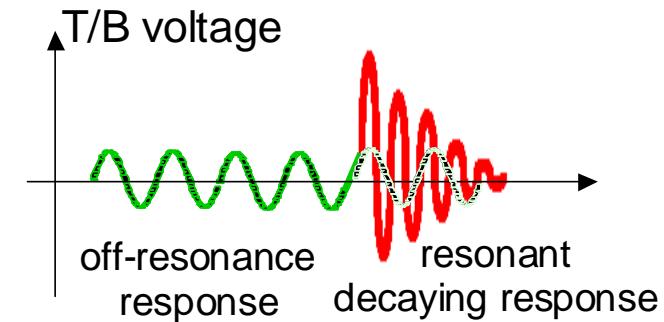
Modelling: Interacting Beams



Assumptions:

- ◆ Impulsive impact of D on T/B
- ◆ Zero engaging time
- ◆ No effect on D by T/B

$$F_{DT,DB} = \begin{cases} 0 & d_{T,B} > 0 \\ f(\dot{y}_{DT,DB}) & d_{T,B} = 0 \end{cases}$$

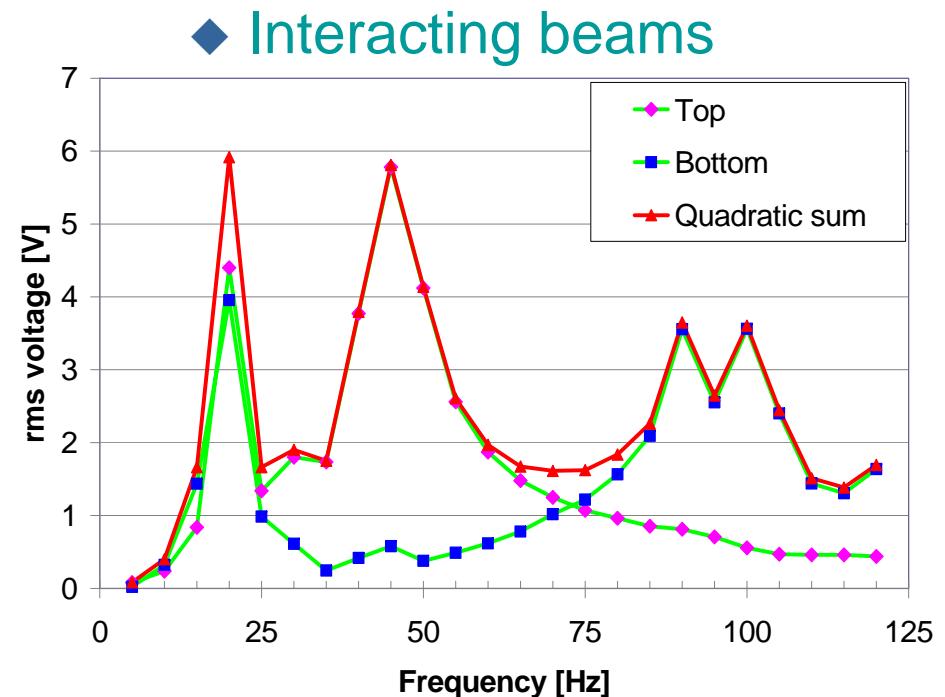
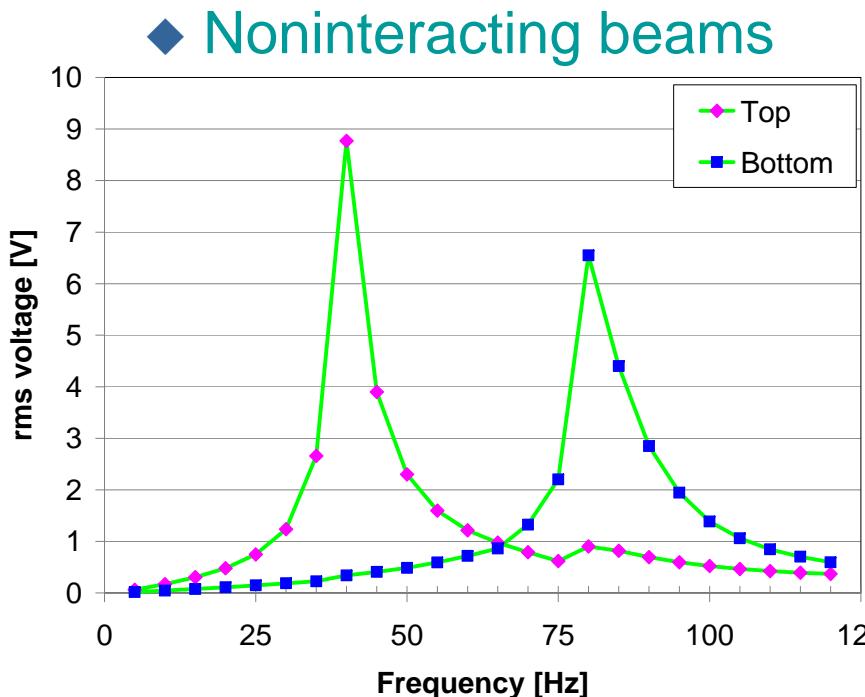


V.Ferrari

London, March 28, 2012

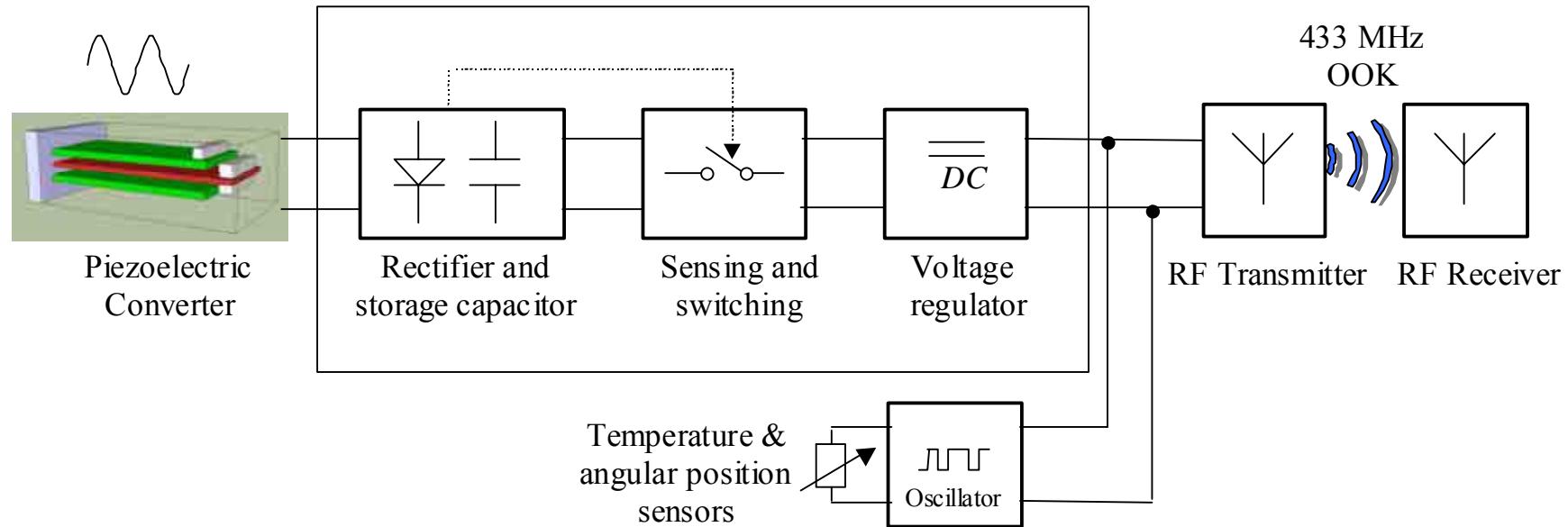
Experimental Results

- EH mounted on the shaker
(Brüel & Kjær Vibration exciter type 4808)
- Swept-frequency excitation
of the shaker
($a_{pk} = 1 \text{ g}$ @ 50 Hz)



- Power on matched load: $1\div 2 \text{ mW}$

Experimental Results



- Handheld EH intentionally shaken
- RF transmissions start after 10 to 15 s and repeat every few seconds under moderate to forcible shaking

F. Cerini
D. Roncalli
University of Brescia



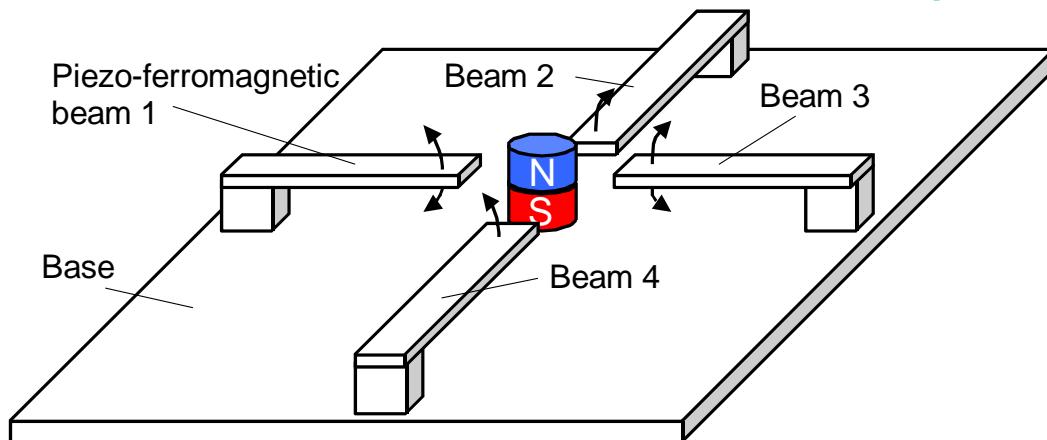
V.Ferrari

London, March 28, 2012

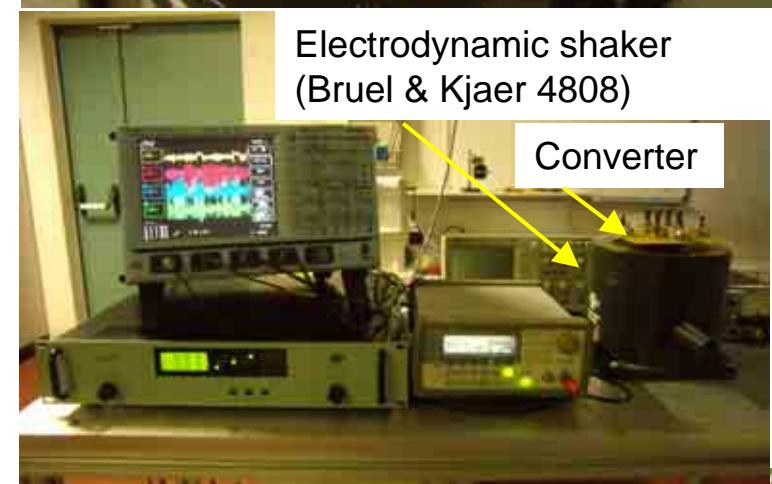
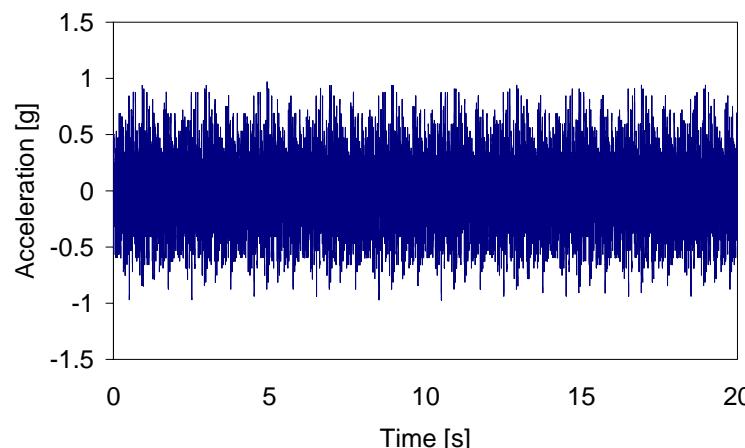


Nonlinear MultiFrequency Array

- MFCA and NL concepts merged into a compact configuration
- The beams have different frequency responses

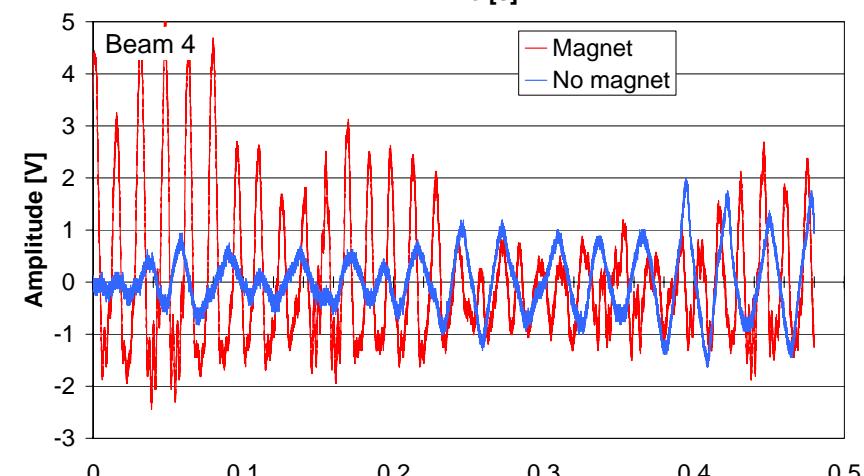
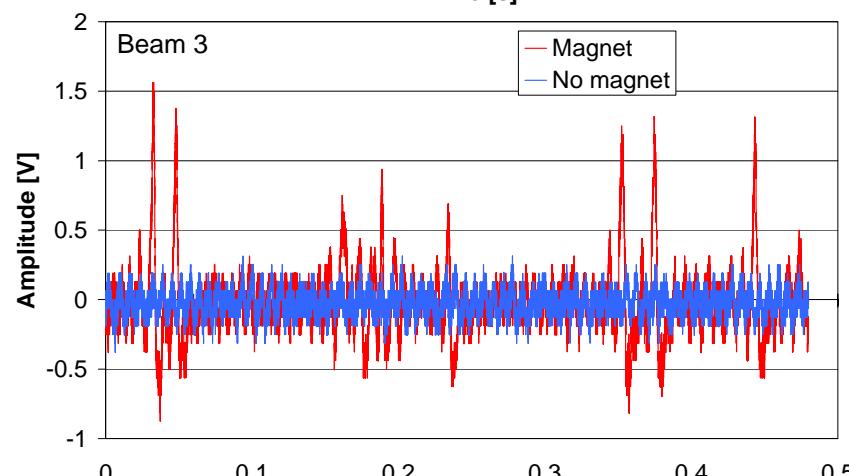
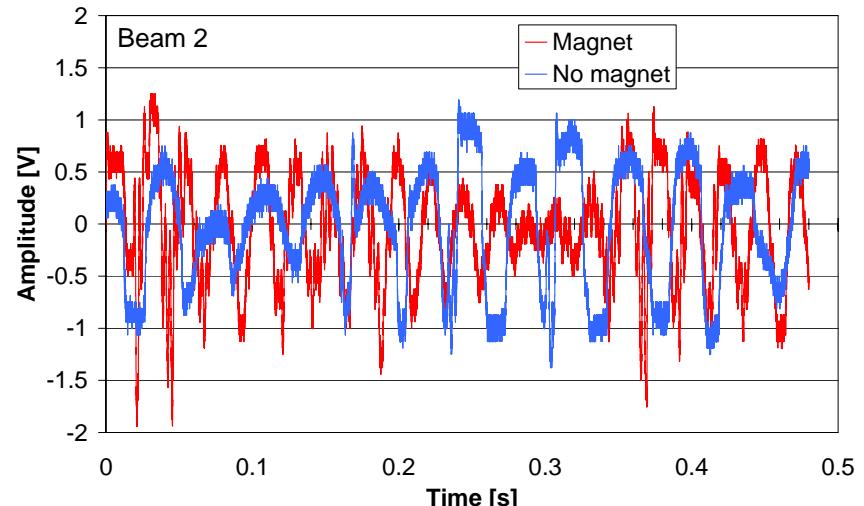
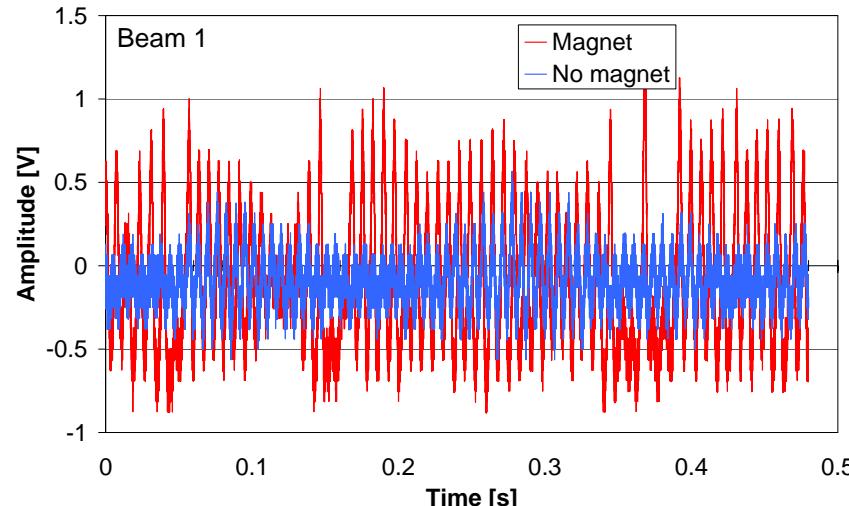


Parameter	Beams 1, 3	Beams 2, 4
Steel thickness [μm]	200	100
Tip mass	no	yes
Res. frequency [Hz]	150	30



Experimental Results

- Typical responses with and without the magnet

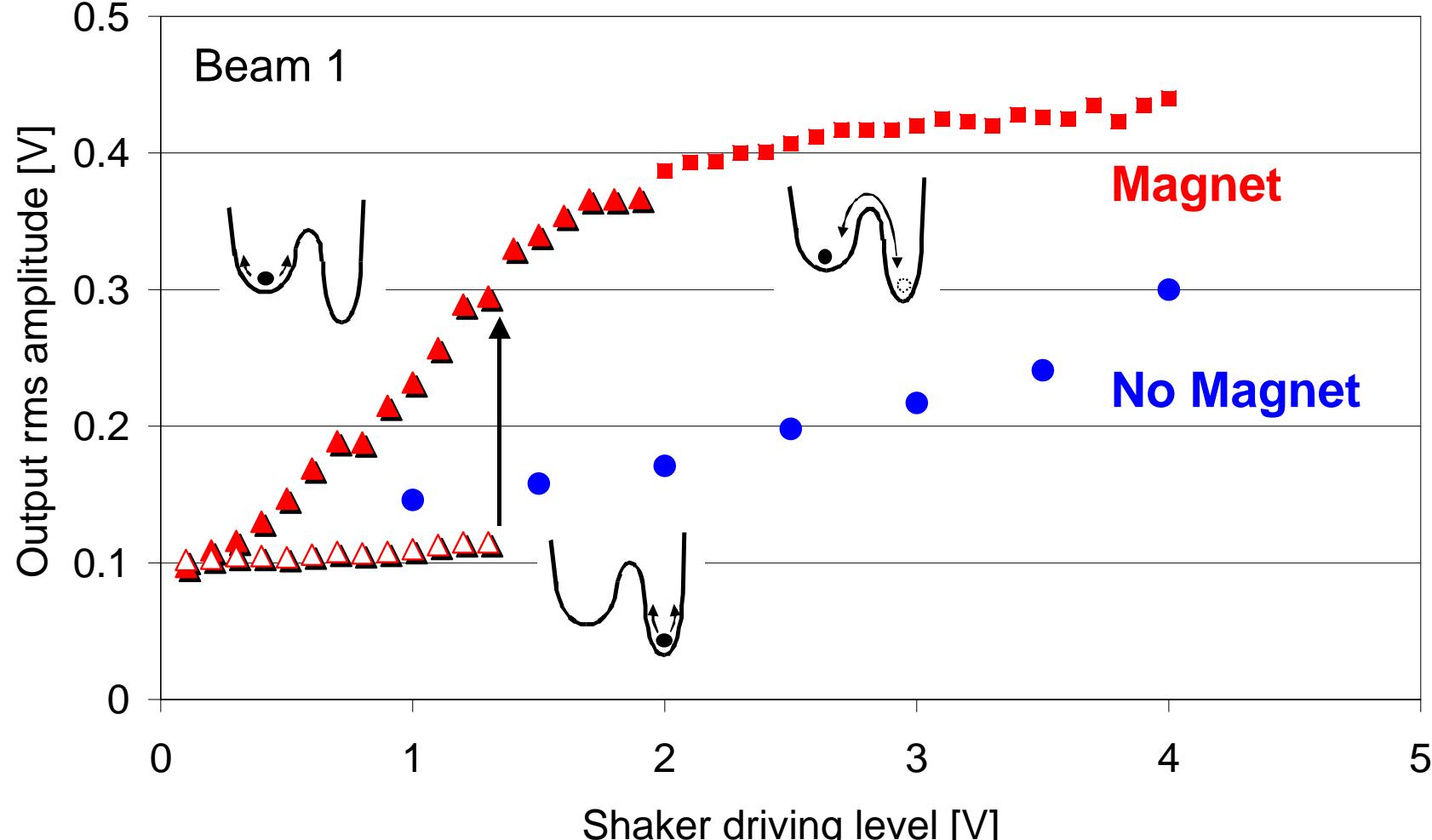


- Complex dynamics: quasi linear, nonlinear, bistable
- In all cases the magnet increases the rms output



Experimental Results

- Typical responses with and without the magnet

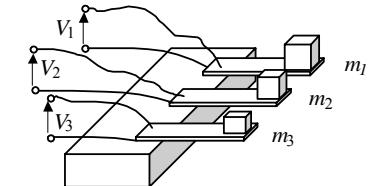


- Complex dynamics: quasi linear, nonlinear, bistable
- In all cases the magnet increases the rms output

Summing Up

- **Linear MFCA harvesters:**

- Bandwidth is not amplitude-sensitive
- Good performances with multi-tone excitations
- Bandwidth is limited by the resonances of the array elements



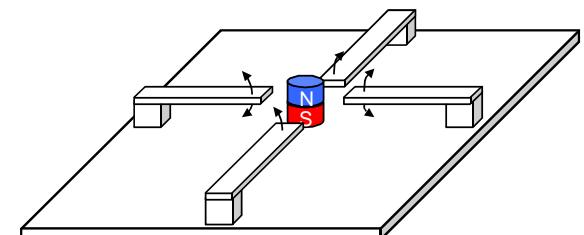
- **Nonlinear (NL) harvesters**

- Bandwidth exceeds the range of linear resonances
- Good performances with random excitations
- Sufficient amplitude is needed for bandwidth expansion



- **NL- MFCA harvesters:**

- Benefits of both classes
- Triggering of nonlinearity/bistability by mutual interactions among converters and magnet(s)



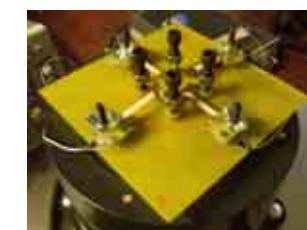
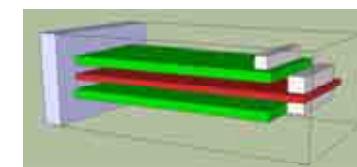
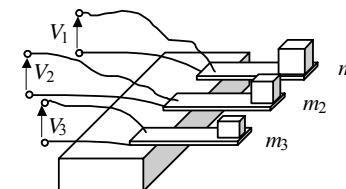
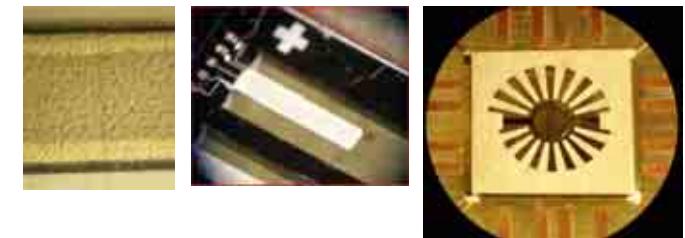
Contents

- Introduction
- Multi-frequency piezoelectric harvester arrays
- Nonlinear piezoelectric harvesters
- Conclusions



Conclusions

- Piezoelectric elements and PZT thick films on different substrates investigated for **energy harvesting**
- Promising approaches studied for energy harvesting from **broadband vibrations**:
 - ◆ Multi-Frequency converter arrays
 - ◆ Nonlinear converters
 - ◆ Nonlinear converter arrays



Acknowledgments

- ◆ T. Zawada and M. Guizzetti at **MEGGIT-Ferroperm (DK)**: collaboration on the piezoelectric materials.
- ◆ P. Colombi at **CSMT - Brescia** for providing sputtering.
- ◆ **MIUR**:
 - ◆ Projects PRIN 20078ZCC92 (2008-2010); PRIN 2009KFLWJA (2011-2013).

