# Miniaturising Motion Energy Harvesters: Limits and Ways Around Them

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### **Inertial Harvesters**

- Mass mounted on a spring within a frame
- Frame attached to moving "host" (person, machine...)
- Host motion vibrates internal mass
- Internal transducer extracts power



### Available Power from Inertial Harvesters

assume:

- source motion amplitude  $Y_o$  and frequency  $\omega$
- Proof mass m, max internal displacement z<sub>o</sub>



- Peak force on proof mass  $F = ma = m\omega^2 Y_o$
- Damper force < F or no movement
- Maximum work per transit  $W = Fz_o = m\omega^2 Y_o z_o$
- Maximum power

 $P = 2W/T = M\omega^3 Y_0 Z_0/\pi$ 



Ref: Mitcheson, P. et al. "Architectures for vibration-driven micropower generators", J. Microelectromechanical Systems 13(3), pp. 429-440 (2004).

## **Implications for Scaling**

- Maximum power  $P = m\omega^3 Y_o z_o / \pi$
- For length dimension L, m scales as L<sup>3</sup>
- Z<sub>o</sub> scales as L
- So power scales as L<sup>4</sup>
- Power density falls as size reduces



### How much power is this?



Plot assumes:

- Si proof mass (higher densities possible)
- max source acceleration 1g (determines Y<sub>o</sub> for any f)

### Achievable Power Relative to Applications



Plot assumes:

- proof mass 10 g/cc •
- source acceleration 1g

## **Possible Power Relative to Batteries**



#### Plot assumes:

- proof mass 10 g/cc
- source acceleration 1g

## **Power Density**

- Depends on geometry: highest P/Vol for travel along long axis
- MEMS devices typically use plate geometry not ideal
- In-plane motion: hard to achieve optimal travel range
- Off-axis travel can be a problem



#### Imperial College London Implementation Issues: Resonance

### Why use resonant device?

Allows use of full internal range for low Y<sub>o</sub>

Why not use resonant device?

- For low frequency application,  $Y_o > z_o$  likely
- Low resonant frequency hard to achieve for small devices
- Not suitable for broadband or varying source frequency

### Imperial College London Implementation Issues: Resonance

Input displacement vs frequency: low frequency range



### Transduction: Electromagnetic



Example: Southampton/Tyndall Inst. Advantages:

- Well understood system
- No source voltage needed (with permanent magnets)

### Disadvantages

- Limited number of winding turns in MEMS: low voltages
- Low damping forces in low frequency operation

### Transduction: Electrostatic



Example: MIT

Advantages:

- No special materials
- Suitable for MEMS scale

### Disadvantages

- Needs priming voltage, or electret
- high output voltages typical

### Transduction: Piezoelectric



### Example: UC Berkeley

Advantages:

- High voltage even at low frequency
- Simple geometries

### Disadvantages

- Low coupling coefficient
- integration of material

### A Non-Resonant Electrostatic Harvester

- Si proof mass: whole wafer etching
- Polyimide suspension: low stiffness
- Wide frequency range of operation: suitable for body motion
- Self-synchronous: physical contact to charging and discharging terminals
- Size ≈ 12 × 12 × 1.5 mm





assembled generator



detail of moving plate

### Imperial College London Non-Resonant Electrostatic Harvester 2





Mass

- Measured output > 2  $\mu$ W at 20 Hz excitation
- Wide operating frequency range

Ref: Miao, P. et al. "MEMS inertial power generators for biomedical applications", Microsystem Techn. 12 (10-11), pp.1079-1083 (2006).

### Non-Resonant Electrostatic Harvester: Problems

- Si density low reduces *m*
- Travel range limited movement is in short dimension
- Whole wafer etching expensive and limits integration potential
- Output in inconvenient large impulses



#### Imperial College London External Mass Electrostatic Harvester

- Proof mass rolls on substrate
- Multiple charge-discharge cycles per transit
- No deep etching: fabrication simplicity
- Large mass and internal travel range

#### But:

- Very low capacitances & capacitance ratios
- Thus, low power for given priming voltage



Schematic illustrating concept

#### Ref:

M. Kiziroglou, C. He and E.M. Yeatman, "Rolling Rod Electrostatic Microgenerator", IEEE Trans. Industrial Electronics **56**(4), pp. 1101-1108 (2009).



**Electrostatic simulation** 



Rolling mass on prototype device

## Overcoming Low Electro-mechanical Coupling: Frequency Up-Converting Piezoelectric Harvester

- External rolling proof mass
- Distributed transduction by series
  of piezo beams
- Proof mass "plucks" beams by magnetic interaction
- Energy extracted as beams ring down: high electrical damping not needed





Ref:

P. Pillatsch, E.M. Yeatman & A.S. Holmes, "Piezoelectric Impulse-Excited Generator for Low Frequency Non-Harmonic Vibrations", Proc. PowerMEMS 2011, Seoul, Nov. 2011, pp. 245-248.

### Frequency Up-Converting Piezoelectric Harvester



4 test configurations:

- a<sub>1</sub> = 2.72 m/s<sup>2</sup>
- $a_2 = 0.873 \text{ m/s}^2$
- m<sub>1</sub> = 0.285 kg
- $m_2 = 0.143 \text{ kg}$

- Operation over a wide frequency range (6:1) demonstrated at higher acceleration
- Effectiveness reasonable for first design
- Power density of 4-13  $\mu W/cm^3$  for lighter proof mass
- Scalable design



### Overcoming Low Electro-Mechanical Coupling: Active Interface Circuits

- Piezo devices limited by high output capacitance
- Difficult to match load impedance leads to weak damping factor
- Concept is to synchronously precharge the piezo cell to increase damping force



### Re-designing Sensor Architecture for Harvester-Powered Operation

- Harvester power density inherently low for low frequency (e.g. human powered) applications
- Traditional architecture based on separate power and other modules
- Data processing and transmission modules most power intensive
- Solution: new approach to node architecture, mixing modules together



### New Architecture

- Harvester connected between sensor output and transmitter
- Sensor acts as priming voltage, harvester as pulse former and energy amplifier
- Output pulses transmitted directly without further processing



### **Fully Assembled Device**

- Input from voltage supply representing output of sensors
- RF frequency determined by size of antenna loop: in this case 350 MHz
- Commercial off-the-shelf TV receiver employed for its broad bandwidth
- Higher frequency ( > 1 GHz) will allow antenna loop close to harvester size (5 mm)





#### Ref:

C. He, M. Kiziroglou, D. Yates and E.M. Yeatman, "A MEMS Self-Powered Sensor and RF Transmission Platform for WSN Nodes", IEEE Sensors **11**(12), pp.3437-3445 (2011).

### Overcoming Displacement Limit: Rotational Harvesters

Inertial Harvesters: power is limited by proof mass and travel range:

Maximum power =  $m\omega^3 Y_o Z_o / \pi$ 

Any alternatives?

yes, rotating proof mass: limited motion range not inherent

Ref:

E.M Yeatman, "Energy Harvesting from Motion Using Rotating and Gyroscopic Proof Masses", J. Mechanical Engineering Science **222** (C1), pp. 27-36 (2008).

### **Rotating Mass Inertial Generator**

### Example #1: traditional self-winding watch



## **Rotating Mass Inertial Generator**

Example #2: Seiko Kinetic





Rotating mass generator – two possible modes:

- driven by linear motion
- driven by rotating motion

Rotating mass generator – two possible modes:

- driven by linear motion
- driven by rotating motion

Semi-circle design of watch proof masses allows the former:

- Theoretically achievable power is similar to linear motion device: relative direction of mass and frame motion reverses on each half turn
- Advantage is in implementation practicalities.

### Rotating mass generator driven by rotating motion

Potential advantage: resonant enhancement

- Allows benefit of "unconstrained" internal amplitude
- Actual constraint is the need for a spring

### Proposal : Rotating mass resonant generator

source motion amplitude  $\theta_{o}$  , frequency  $\varpi$  proof mass m, radius R

Achievable power:

 $=\frac{mR^2\theta_o^2\omega^3}{8}\sqrt{\frac{mR^2}{8}}$  $\overline{Q}$  $P_{\rm max}$ 



### Compare: Rotating vs Linear resonant generator

Example: upper limb swinging at 1 Hz

- Linear:  $Y_o = 5$  cm
- Rotating:  $\theta_0 = 25 \text{ deg}$
- Use mass of 1 g, radius = travel range = 0.5 cm

$$P_{\max} = \frac{mY_o Z_o \omega^3}{\pi} \qquad \text{vs.} \qquad P_{\max} = \frac{mR^2 \theta_o^2 \omega^3}{8} \sqrt{Q}$$

Result:  $P_{lin} = 13 \text{ uW}$   $P_{rot} = 0.2 \text{ uW} \sqrt{Q}$  Imperial College London Rotating vs Linear resonant generator

$$P_{lin} = 13 \text{ uW}$$
  $P_{rot} = 0.2 \text{ uW} \sqrt{Q}$ 

 $P_{rot}$  higher for Q > 4000

Technical Challenge:

 High Q for resonant rotating device requires spring with very high number of turns

**Practical Challenge:** 

• High Q means high drive frequency dependence

### **Overcoming the Mass Limit**

How else can rotating motion be used in inertial generation?

### **Overcoming the Mass Limit**

How else can rotating motion be used in inertial generation?

What about driving the rotation actively?

### Proposal: Gyroscopic power generation



### **Imperial College** Gyroscopic power generation

London

Basic principle: for moment of inertia I rotating at  $\omega_s$  and tipped at  $\omega_p$ : torque T =  $I\omega_s\omega_p$ 



### Gyroscopic power generation

Mechanism: couple the rocking frame to the gyroscopic body by the energy extracting damper (electrostatic...)

For disk spun at  $\omega_{\rm s}$  and rocked at  $\omega_{\rm o},$  achievable power:

 $P_{gyr} = \frac{1}{4} m R^2 \theta_o^2 \omega_o^2 \omega_s$ 



### Gyroscopic power generation

Opportunity: power output rises with spin speed

Limitation: need to subtract drive power

• Depends on drive speed; optimum drive speed thus determined by Q

### Gyroscopic power generation

Net power:

 $P_{gyr} = \frac{\sqrt{2\pi/3}}{3} m R^2 \theta_o^2 \omega^3 \sqrt{Q}$ 

About 4x resonant rotating (passive) case

### Gyroscopic power generation



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How to implement in MEMS? High quality spinning bearings not really available.

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How to implement in MEMS? High quality spinning bearings not really available.

- Solution: well known format for MEMS gyros
  - Vibrating gyro



### Imperial College London Gyroscopic power generation

- Proposed format: linear vibration on two axes, one for drive, one for pickoff;
- Same as gyro sensor except pick-off extracts energy, not signal



after Fedder et al

### Conclusions

- Basic mechanics sets strict limits on achievable power from inertial harvesters
- Ultimate power density drops as devices shrink
- Form factor, resonance and choice of transduction are important considerations
- Rotating harvesters can offer some ways around the basic limits

#### Thanks:

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*Review Paper:* P. D. Mitcheson, E. M. Yeatman, G.K. Rao, A. S. Holmes & T. C. Green, "Energy Harvesting from Human and Machine Motion for Wireless Electronic Devices", Proc. IEEE 96(9), pp. 1457-1486 (2008).